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13. ABSTRACT (Maximum 200) The objective of the proposed research is to develop computer-aided diagnosis methods for use in mammography in order to increase the diagnostic accuracy of radiologists and to aid in mammographic screening programs. We have increased the detection accuracy of our computerized method by incorporating temporal information and by developing a new single-image detection method. We have also investigated methods for feature selection and feature merging (classifiers) when only limited datasets are available. We have also continued to implement and investigate the use of our clinical prototype intelligent workstation.				
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FOREWORD

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Table of Contents

	Page
FRONT COVER.....	1
STANDARD FORM (SF 298).....	2
FOREWORD.....	3
INTRODUCTION	5
BODY	6
KEY RESEARCH ACCOMPLISHMENTS	11
REPORTABLE OUTCOMES	11

INTRODUCTION

Our first-year report was accepted as an excellent report as submitted. The review of our first year report indicated that the report was well-written with extensive background material and meticulous description of the theoretical basis for the algorithms, which are not necessary in future annual reports and could be referred to with appropriate citations. Thus, in this third-year report, we have substantially shortened the background sections and refer the reviewer to our first-year report, especially now that the report be 2-5 pages only.

Although mammography is currently the best method for the detection of breast cancer, between 10-30% of women who have breast cancer and undergo mammography have negative mammograms. In approximately two-thirds of these false-negative mammograms, the radiologist failed to detect the cancer that was evident retrospectively. Low conspicuity of the lesion, eye fatigue and inattentiveness are possible causes for these misses. We believe that the effectiveness (early detection) and efficiency (rapid diagnosis) of screening procedures could be increased substantially by use of a computer system that successfully aids the radiologist by indicating locations of suspicious abnormalities in mammograms. In addition, many breast cancers are detected and referred for surgical biopsy on the basis of a radiographically detected mass lesion or cluster of microcalcifications. Although general rules for the differentiation between benign and malignant breast lesions exist, considerable misclassification of lesions occurs with the current methods. On average, only 10-30% of masses referred for surgical breast biopsy are actually malignant. Surgical biopsy is an invasive technique that is an expensive and traumatic experience for the patient and leaves physical scars that may hinder later diagnoses (to the extent of requiring repeat biopsies for a radiographic tumor-simulating scar). A computerized method capable of detecting and analyzing the characteristics of benign and malignant masses, in an objective manner, should aid radiologists by reducing the numbers of false-positive diagnoses of malignancies, thereby decreasing patient morbidity as well as the number of surgical biopsies performed and their associated complications.

Purpose of the present work

The main hypothesis to be tested is that given dedicated computer-vision programs for the computer-assisted interpretation of mammograms, the diagnostic accuracy for mammographic interpretation will be improved, yielding earlier detection of breast cancer (i.e., a reduction in the number of missed lesions) and a reduction in the number of benign cases sent to biopsy. Computer-aided diagnosis (CAD) can be defined as a diagnosis made by a radiologist who takes into consideration the results of a computerized analysis of radiographic images and uses them as a "second opinion" in detecting lesions and in making diagnostic decisions. The final diagnosis would be made by the radiologist.

Methods of approach

The objective of the proposed research is to develop computer-aided diagnosis methods for use in mammography in order to increase the diagnostic decision accuracy of radiologists and to aid in mammographic screening programs. The CAD methods will include a parallel method for the detection of a range of mass types and for the incorporation of information from multiple views (i.e., CC and MLO, and prior mammograms).

The **specific objectives** of the research to be addressed are:

- (1) Development of advanced computerized schemes for the detection and classification of masses in digital mammograms.
 - (a) Development of a computerized detection scheme for spiculated lesions and architectural distortions based on the calculation of the Hough spectrum.

(b) Development of a computerized detection scheme for small, low-contrast early cancers based on gradient and circularity filters.

(c) Incorporation of the two new methods with a previously-developed bilateral-subtraction method along with feature analyses into a system for lesion detection.

(d) Further development of computerized classification schemes for masses.

(2) Development of computerized methods based on multiple views for enhanced mammographic interpretation.

(a) Development of computerized methods for the incorporation of image information from the CC and MLO views of mammographic examinations.

(b) Development of computerized methods for analysis of temporal change between mammographic examinations.

(3) Incorporation of the computer-vision methods with an Mammo/Icon mammographic review system for enhanced diagnosis.

(a) Expansion of the Mammo/Icon database descriptors to include CAD derived parameters.

(b) Calculation of the computer extracted features of images in the Mammo/Icon database.

(c) Development of hardware and software interfaces for CAD and Mammo/Icon.

(4) Evaluation of the CAD methods for mammography.

BODY

Development of advanced computerized schemes for the detection of masses in digital mammograms. Results to date

With the single-image method for detection of small invasive breast cancers localized density peaks on mammograms are identified using a gradient/circularity filter. Lesion contours were generated by matching a deformable template onto a second derivative edge map. In a preliminary study (without further feature analyses to reduce false positives) using 45 non-palpable invasive breast cancers, all with a size less than 1 cm (median size of 7 mm), 82% of the cancers were detected with an average false-positive rate of 2.8 per image.

In the Hough spectrum geometric texture analysis technique, the mammogram is analyzed ROI by ROI. Each ROI is transformed into its Hough spectrum and then thresholding is performed with its threshold level based on the statistical properties of the spectrum. ROIs with strong signals of spiculation are then screened out as regions of potential lesions. In a preliminary study, 32 images containing spiculated lesions/architectural distortions (biopsy confirmed) were analyzed using information extracted from the Hough spectrum. Our preliminary studies, using only the Hough spectrum based technique without further feature analyses to reduce false positives, yielded sensitivities of 81% for spiculated masses and 67% for architectural distortions at false positives rates of 0.97 and 2.2 per image, respectively. We have also converting the method into an AVS based program to expedite the development and optimization of the parameters such as ROI size.

Output from the bilateral subtraction method and that of the gradient/circularity filtering were combined and analyzed. Many masses were detected by both preprocessing methods. For a database of 20 cancer cases, the bilateral yielded a sensitivity of 75% (at 1.8 false-positives detections per image) and the gradient/circularity filter yielded a sensitivity of 70% at the same false positive rate. Upon comparison, the gradient/circularity filter found masses that the bilateral did not, thus allowing the sensitivity to increase to 80%. We are currently comparing the false positive overlap to determine the false-positive rate for the combined scheme as well as give us a means to improve the false-positive rate while optimizing the sensitivity for each method.

Since November 8, 1994, all screening mammograms taken at the University of Chicago Hospitals have been analyzed on our clinical prototype mammography workstation, except during downtimes. Downtime has been minimal, less than 20 days in total, which includes a 3-week period when the

mammography section moved to a new outpatient center. During that move, networking problems in the new facility contributed to computer system difficulties. For cases in which a cancer was detected, we also retrospectively reviewed any previous mammograms that were in our study cohort. Two radiologists independently reviewed the cases and stated whether the cancer was visible in a previous exam and whether, knowing that the lesion was present, that they would call the patient back for a diagnostic exam based on the findings in the previous exam. In this way, the number of cancers detected by the computer that were initially missed by the radiologists was determined. As of May, 1, 1998, over 14,000 cases have been analyzed. With follow-up on the first 10,000 cases, 61 patients have been diagnosed with breast cancer. In 12 of these cases, the screening mammogram(s) were negative even in retrospect. For the mammographically visible cases ($n=49$), the sensitivity of the two schemes was 68% (34/49). Clinically, 96% of the cancers were detected (47/49). More important than the absolute sensitivity of the workstation is its ability to detect breast cancers that may be missed by a radiologist. In 30 of the 61 cancers, the patient had a screening exam that was read as negative and was included in our study. That is, a screening mammogram that was read as normal, which preceded the cancer being diagnosed. In 14 of these cases, no lesion could be seen in retrospect, i.e., mammographically negative. In 9 of 16 cases, the computer was able to identify the region on the negative-read (cancer visible in retrospect) screening mammogram that corresponded to where the cancer was subsequently detected. Overall, the computer was able to identify the cancer approximately one year before it was diagnosed in approximately 15% (9/61) of all cancer cases and in 56% (9/16) of cases where the cancer was visible in retrospect on a negative-read screening mammogram. The false-positive rate was approximately 1.3 false clusters per image and 2.1 false masses per image. The types of false-positive detections found by the computer in mass detection and clustered microcalcification detection were investigated for 1296 cases. Of the false positives that were indicated by the computer, over 80% of the mass false positives were due to nodular densities on the film.

In order to determine the effect of false-positive detections on mammographic interpretation, we calculated the call-back rate in one-year time periods before and after implementation of the workstation in the clinical area. The callback rate is the fraction of screening mammograms read as abnormal. Before introduction of CAD, 13.2% of screeners were called back for further workup and after the introduction of CAD, 12.6% of screeners were called back for further workup. Thus, the false-positive output from the computer did not increase the number of women called back.

A new development, which is now being implemented into the various detection and classification schemes for mammographic masses, is a new region growing algorithm. The segmentation of lesions from surrounding background is a vital step in many computerized mass detection schemes. We have developed two novel lesion segmentation techniques -- one based on a single feature called the radial gradient index (similar feature to that described above) and one based on a simple probabilistic model to segment mass lesions from surrounding background. In both methods a series of image partitions is created using gray-level information as well as prior knowledge of the shape of typical mass lesions. With the former method the partition that maximizes the radial gradient index is selected. In the latter method, probability distributions for gray-levels inside and outside the partitions are estimated, and subsequently used to determine the probability that the image occurred for each given partition. The partition that maximizes this probability is selected as the final lesion partition (contour). We tested these methods against our previous region-growing algorithm using a database of biopsy-proven, malignant lesions and found that the new lesion segmentation algorithms more closely match radiologists' outlines of these lesions. At an overlap threshold of 0.30, gray level region growing correctly delineates 62% of the lesions in our database while the radial gradient index (RGI) algorithm and the probabilistic segmentation algorithm correctly segment 92% and 96% of the lesions, respectively. With these new segmentation results we hope to find and extract new features that will help differential between actual lesions and false-positive detections, thus improving the overall performance of computerized mass detection.

A new extension of the region growing method was developed. The radial gradient index (RGI) region growing method is now being implemented at the very first stage of the mass detection

algorithm in order to increase the sensitivity for mass detection. Thus, this RGI algorithm replaces the bilateral subtraction methodology in the overall computerized mass detection method. The benefit of this change is that cases with unilateral mammograms can be analyzed by the computer method. In addition, the sensitivity of the detection algorithm increased by 15%.

In order to improve the classifier performance in the detection method for distinguishing between actual lesions and false-positive detections, we investigated feature selection with limited datasets and the use of probabilistic artificial neural networks. In many computerized schemes, numerous features can be extracted to describe suspect image regions. A subset of these features is then employed in a data classifier to determine whether the suspect region is abnormal or normal. Different subsets of features will, in general, result in different classification performances. A feature selection method is often used to determine an "optimal" subset of features to use with a particular classifier. A classifier performance measure (such as the area under the receiver operating characteristic (ROC) curve) must be incorporated into this feature selection process. With limited datasets, however, there is a distribution in the classifier performance measure for a given classifier and subset of features. We investigated the variation in the selected subset of "optimal" features as compared with the true optimal subset of features caused by this distribution of classifier performance. We considered examples in which the probability that the optimal subset of features is selected can be analytically computed. We showed the dependence of this probability on the dataset sample size, the total number of features from which to select, the number of features selected, and the performance of the true optimal subset. Once a subset of features has been selected, the parameters of the data classifier must be determined. We showed that, with limited datasets and/or a large number of features from which to choose, bias is introduced if the classifier parameters are determined using the same data that were employed to select the "optimal" subset of features.

It is well understood that the optimal classification decision variable is the likelihood ratio or any monotonic transformation of the likelihood ratio. An automated classifier which maps from an input space to one of the likelihood ratio family of decision variables is an optimal classifier or an ideal observer. Artificial neural networks (ANNs) are frequently used as classifiers for many problems. In the limit of large sample sizes, an ANN approximates a mapping function which is a monotonic transformation of the likelihood ratio, i.e., it estimates an ideal observer decision variable. The disadvantages of conventional ANNs include the potential over-parameterization of the mapping function which results in a poor approximation of an optimal mapping function for smaller sample sizes. Recently, Bayesian methods have been applied to ANNs in order to regularize training to improve the robustness of the classifier. A Bayesian ANN should thus better approximate the optimal decision variable given small sample sizes. We have evaluated the accuracy of Bayesian ANN models of ideal observer decision variables as a function of the number of hidden units used, the signal-to-noise ratio of the data, and the number of features or dimensionality of the data. We showed that when enough training data are present, excess hidden units do not substantially degrade the accuracy of Bayesian ANNs. The minimum number of hidden units required to best model the optimal mapping function, however, varies with the complexity of the data.

Development of advanced computerized schemes for the classification of masses in digital mammograms. Results to date

We are investigating the potential usefulness of computer-aided diagnosis as an aid to radiologists in the characterization and classification of mass lesions in mammography. Ninety-five mammograms containing masses from 65 patients were digitized. Various features related to the margin, shape and density of each mass were extracted automatically from the neighborhoods of the computer-identified mass regions. Selected features were merged into an estimated likelihood of malignancy using three different automated classifiers. The performance of the three classifiers in distinguishing between benign and malignant masses was evaluated by receiver operating characteristic (ROC) analysis, and compared with those of an experienced mammographer and of five less experienced mammographers.

Our computer classification scheme yielded an A_z value of 0.94, similar to that of an experienced mammographer ($A_z=0.91$) and statistically significantly higher than the average performance of the radiologists with less mammographic experience ($A_z=0.80$). With the database we used, the computer scheme achieved, at 100% sensitivity, a positive predictive value of 83%, which was 12% higher than that of the experienced mammographer and 21% higher than that of the average performance of the less experienced mammographers at a p -value of less than 0.001. Thus, automated computerized classification schemes may be useful in helping radiologists distinguish between benign and malignant masses.

We have also investigated the effect of dominant features on neural network performance in the task of classification of mammographic lesions. Two different classifiers, an artificial neural network (ANN) and a hybrid system (one step rule-based method followed by an artificial neural network) were investigated to merge computer-extracted features in the classification of malignant and benign masses. Four computer-extracted features were used in the study: spiculation, margin sharpness and two density-related measures. ROC analysis showed that the hybrid system performed significantly better than the ANN method at the high sensitivity levels, yielding an A_z of 0.94 with a specificity of 69% at 100% sensitivity, whereas, the ANN method yielded an A_z of 0.90 with a specificity of 19% at 100% sensitivity. To understand the difference between the two classifiers in their performance, we investigated their learning and decision-making processes by studying the relationships between the outputs and input features. The correlation study showed that the outputs from the ANN alone method strongly correlated with one of the input features (spiculation measure), yielding a correlation coefficient of 0.91 while the correlation coefficients (absolute value) for the other features range from 0.19 to 0.40. The strong correlation between the ANN output and spiculation measure indicates the learning and decision-making processes of the ANN alone method was dominated by the spiculation measure. A series of three-dimensional plots of the computer output as functions of the input features demonstrate that the ANN method did not learn as effectively as the hybrid system from the other three features in differentiating subtle (non-spiculated) malignant masses from benign masses, thus, resulting in the inferior performance at the high sensitive levels. We found that with a limited database, it is detrimental for an ANN to learn the significance of other features in the presence of a dominant feature. The hybrid system, which initially applied a rule on the spiculation measure prior to an ANN, prevents the over-learning from the dominant feature and performed better than the ANN alone method in merging the computer-extracted features into a correct diagnosis on the malignancy of the masses.

Currently in mammography, the digital image on which CAD analysis is performed is obtained by digitizing a screen-film mammogram. Since the image is sampled when digitized, the digitization of a image using two different scanners will not produce exactly the same digital image (because of different designs, sampling aperture, sampling distance and internal electronic noise, etc. of the laser scanners and the different calibration curves for the transformation of the optical density (OD) to pixel value). Thus, the contrast, noise and resolution of the two images may differ. Thus, as long as CAD analysis relies upon digitized screen-film images, a CAD system (film digitization and computer analysis) may suffer from the variability in the digital formats of a image, which may lead to variations in the performance of the CAD scheme. Two different databases and three different digitizers were involved in this study. One database consisted of 95 mammograms collected from 65 cases: 39 biopsy-confirmed malignant cases, 25 biopsy-confirmed benign cases and one benign case which was determined through more than five years of follow-up. These mammograms were digitized using an optical drum scanner (FIP II, Fuji Film, Tokyo, Japan) at a sampling distance of 0.1 mm and 10-bit quantization. Another database consisted of 110 new cases which were collected from the University of Chicago Radiology files. Of these, 50 cases are biopsy-confirmed malignant, 50 cases are biopsy-confirmed benign diseases and 10 cases are aspiration-confirmed cysts. For each case, two standard views of the affected breast were chosen from a single screening exam. Of the 110 cases, 8 cases had a mass appearing on one view only. Each mammogram this second database was digitized twice using two different laser scanners -- a Konica digitizer (LD 4500; Konica Medical, Wayne, NJ) at 0.1-mm pixel size and 10-bit quantization and a Lumisys laser scanner (Lumiscan 100, Lumisys, Sunnyvale,

CA) at a 0.1-mm pixel size and 12-bit quantization. In the evaluation of our classification scheme, both A_z and ${}_{0.90}A'_z$ are important indices. The A_z value was used to evaluate the overall performance, while the partial area index (${}_{0.90}A'_z$) was designed to evaluate the performance of a scheme at a preselected high sensitivity level for those who are interested in knowing the performance at the high sensitivity. In addition, the difference in the partial area index ${}_{0.90}A'_z$ quantitatively evaluates, to some degree, the difference in the shape of the two ROC curves. The differences in A_z between the two digital formats were the same for both the ANN-alone and hybrid classifiers. Two-tailed p values obtained from the CLABROC programs showed that the difference in the performance of the classification scheme, due to the difference between the two digitization techniques, using both the ANN and the hybrid classifier were not statistically significant at the level of 0.05 in terms of the A_z and ${}_{0.90}A'_z$.

In order to observe the effect of the computer aid on radiologists' performance in the task of distinguishing between malignant and benign lesions, we performed an observer study at RSNA '98. The mass classification method was run on both the MLO and CC views and the magnification views. We showed that the average performance of 128 radiologists (who participated in the study) increased significantly from an A_z of 0.89 to an A_z of 0.94 ($p < 0.05$) when the computer aid was used in distinguishing 20 mass lesions cases.

Development of computerized methods based on multiple views for enhanced mammographic interpretation. Results to date

We have evaluated the potential benefit of incorporating a temporal subtraction scheme with our bilateral subtraction technique for improving the sensitivity of mass detection. A database of 79 cases was used, each of which contained a lesion in at least the current exam. Two methods for image registration of the temporal images were investigated: one used translation and rotation based on computer-determined skin lines and the other used a warping technique based on the cross-correlation of regions of interest located throughout the parenchyma. The characteristics of the false-positive detections resulting from the bilateral subtraction and from the temporal subtraction were analysed. The distribution of the true positives and false positives were similar despite the fact that many of the false positives resulting from the two schemes were in different locations in the breast parenchyma. At a false-positive rate of four per image, the combined (Logical OR) scheme detected 85% of the masses, which was 8% greater than the bilateral subtraction technique alone. Although further work is needed to reduce the false-positive rate, the combined use of bilateral and temporal subtraction methods shows potential for an improvement in sensitivity in the detection of masses.

We are investigating how the lesion features as calculated from the CC, MLO, and magnification views vary. To date we have collected approximately 150 cancer cases from digitized films. Spiculation has been shown to be a dominate feature and is influenced by linear-shaped parenchymal structures that transverse the lesion on the 2-D projection image. This is one of the reasons radiologists prefer to have a computer rating given per view as opposed to per case – since the projected view of a lesion and a linear parenchymal pattern could lead to an erroneous increase in the degree of spiculation as calculated by the computer method. It is important that radiologists understand what features the computer is "looking" at and understand is the computer under-or over calls a lesion.

Incorporation of the computer-vision methods with an Mammo/Icon mammographic review system for enhanced diagnosis. Results to date

Dr. Swetts at Yale has left academics and gone into private practice in Seattle. No grant funds have been transferred to him. Instead researchers on the team at the University of Chicago are creating an "Mammo/Icon-like" system. The features (as well as the merged values from the artificial neural

network) from the malignant and benign cases are tabulated and retained in the computer. We are currently developing software to first retrieve lesions with similar ANN outputs. Next we will develop the methods to retrieve lesions with similar individual features – for example, spiculated vs. non-spiculated or for non-spiculated lesions: low density vs. high density lesions.

Evaluation of the CAD methods for mammography Results to date

Databases are continuously being collected. For mass detection, we have approximately 150 clinical cases of malignant masses. New data for the classification database includes the 150 malignant cases as well as 100 benign cases. The complete statistical evaluation will be performed at a later date when the databases are complete.

We have evaluated the mass classification method at RSNA 98. The mass classification method was run on both the MLO and CC views and the magnification views. We showed that the average performance of 128 radiologists (who participated in the study) increased significantly from an A_z of 0.89 to an A_z of 0.94 ($p < 0.05$) when the computer aid was used in distinguishing 20 mass lesions cases.

KEY RESEARCH ACCOMPLISHMENTS

1. Improvements in the computerized detection of mass lesions on mammograms
 - Incorporation of temporal image data
 - Development of new single image detection method instead of bilateral subtraction
2. Improvements in the computerized classification of mass lesions on mammograms
 - Investigation of a hybrid (rule-based plus ANN) system for classification
 - Validation on an independent database showing robustness of the method
3. Development of a new lesion extraction (region growing) method
4. Investigation into feature selection and feature merging with limited datasets
5. Continued experience with a clinical “prototype” intelligent workstation

REPORTABLE OUTCOMES

1. Nishikawa RA, Giger ML, Wolverton DE, et al: Prospective testing of a clinical mammography workstation for CAD: Analysis of the first 10,000 cases. Digital Mammography '98. Proceedings of the 4th International Workshop of Digital Mammography, The Netherlands, (in press), 1998.
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Automated Seeded Lesion Segmentation on Digital Mammograms

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Abstract—Segmenting lesions is a vital step in many computerized mass-detection schemes for digital (or digitized) mammograms. We have developed two novel lesion segmentation techniques—one based on a single feature called the radial gradient index (*RGI*) and one based on simple probabilistic models to segment mass lesions, or other similar nodular structures, from surrounding background. In both methods a series of image partitions is created using gray-level information as well as prior knowledge of the shape of typical mass lesions. With the former method the partition that maximizes the *RGI* is selected. In the latter method, probability distributions for gray-levels inside and outside the partitions are estimated, and subsequently used to determine the probability that the image occurred for each given partition. The partition that maximizes this probability is selected as the final lesion partition (contour). We tested these methods against a conventional region growing algorithm using a database of biopsy-proven, malignant lesions and found that the new lesion segmentation algorithms more closely match radiologists' outlines of these lesions. At an overlap threshold of 0.30, gray level region growing correctly delineates 62% of the lesions in our database while the *RGI* and probabilistic segmentation algorithms correctly segment 92% and 96% of the lesions, respectively.

Index Terms—Computer-aided diagnosis, digital mammography, lesion segmentation, mass detection.

I. INTRODUCTION

THE University of Chicago is currently developing computerized schemes to detect mass lesions in digital (or digitized) mammograms [1]–[3]. Many computerized schemes initially return a number of locations called “potential lesion” sites. These are regions that the computer deems suspicious and require a closer examination. A lesion segmentation algorithm is then employed to extract the lesion or potential lesion from its surrounding tissues. Features can then be calculated using the segmentation information and classification can be accomplished using these features [4].

Numerous techniques have been developed to segment lesions from surrounding tissues in digital mammograms. Petrick *et al.* [5] employed density-weighted contrast enhancement (DWCE) segmentation algorithm to extract lesions and

potential lesions from their surrounding tissues. Comer *et al.* [6] and Li *et al.* [7] used Markov random fields to classify the different regions in a mammogram based on texture. A lesion segmentation algorithm was developed by Sameti *et al.* [8] used fuzzy sets to partition the mammographic image data. Despite the difficulty and importance of this step in many computerized mass-detection schemes, few have attempted to analyze the performance of these segmentation algorithms alone, choosing instead to collectively analyze all components of a scheme.

In this paper, we present two methods for segmenting lesions in digital or digitized mammograms: a radial gradient index (*RGI*)-based algorithm and a probabilistic algorithm. These techniques are seeded segmentation algorithms; they begin with a point, called the seed point, which is defined to be within the suspect lesion. Many current computerized mass-detection schemes first employ an initial detection algorithm which returns locations that are used as seed points for the segmentation algorithm. In our previous research [4], a region growing algorithm [9], [10] was performed to extract the lesion from its surrounding tissues. Region-growing is a local thresholding process which utilizes only the gray-level information around the seed point. A series of partitions containing the seed point is created by thresholding, and rules (relating to size and circularity, for example) determine which partition best segments the suspect lesion. Potential problems with such methods are that the rules devised to choose the suspect lesion's partition are heuristic and often based on the first or second derivatives of noisy data. The new methods discussed in this paper attempt to solve the problems associated with conventional region growing by utilizing shape constraints to regularize the partitions analyzed, and simplifying the partition selection process by using utility functions based either on a single feature or probabilities. The performance of the two methods is compared against radiologists' outlines on a screening database of malignant lesions.

II. LESION SEGMENTATION

Given a subimage or region-of-interest (ROI) of dimension n by m containing the suspect lesion, we define the set of coordinates in this subimage as

$$\mathcal{I} = \{(x, y) : x = 1, 2, \dots, n \text{ and } y = 1, 2, \dots, m\}. \quad (1)$$

The function describing the pixel gray levels of this subimage is given by $f(x, y)$ where $(x, y) \in \mathcal{I}$. The values of $f(x, y)$,

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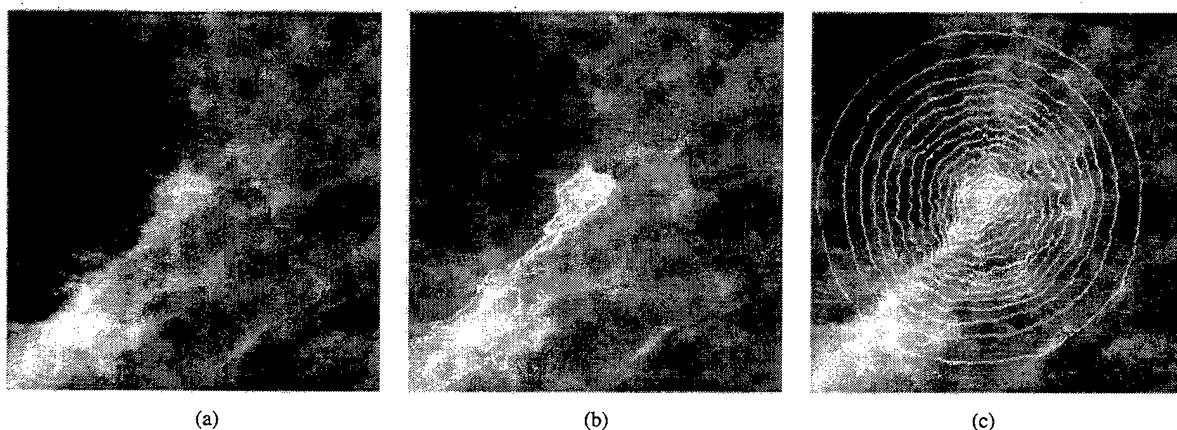


Fig. 1. Partitions that can arise (b) when only gray-level information, $f(x, y)$ is utilized in segmenting lesions and (c) when the gray-level image is multiplied by a constraint function to control the shape of the partitions, $h(x, y)$. The original image is shown in (a).

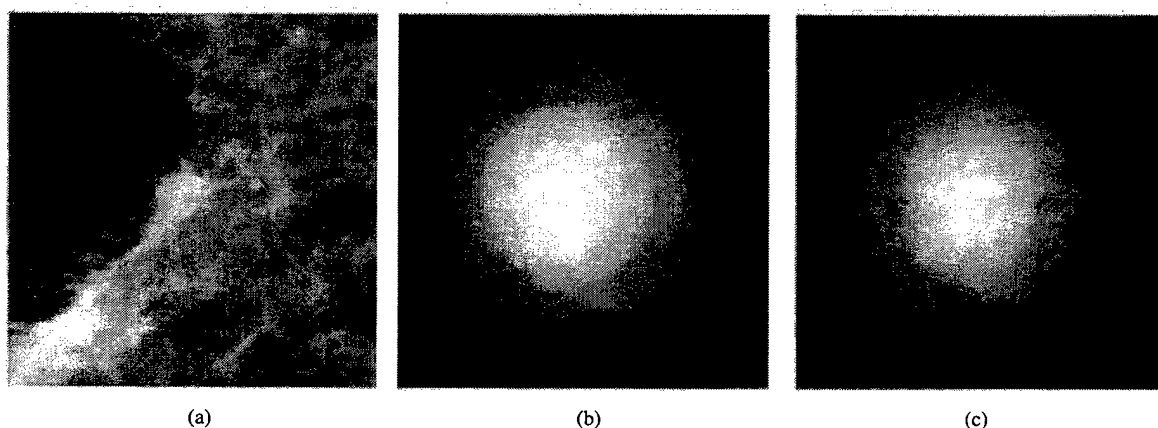


Fig. 2. The image (a) $f(x, y)$ of the lesion is multiplied by the Gaussian function (b) $N(x, y; \mu_x, \mu_y, \sigma_c^2)$ to constrain the partitions to have "lesion-like" shapes, which results in (c) the function $h(x, y)$. The value of σ_c^2 was set to 12.5^2 mm^2 for these images.

for this work, are bound between zero and one, with a zero representing black and a one representing white. The pixel values for all images were normalized to be within this range by dividing by the maximum pixel value possible for the digitizer used. The task of a lesion segmentation algorithm is to partition the set \mathcal{I} into two sets: \mathcal{L} which contains the coordinates of lesion pixels, and $\sim\mathcal{L}$ which contains surrounding background pixels. The lesion segmentation algorithms described in this paper are seeded segmentation algorithms; an initial point is used to start the segmentation. The seed point (μ_x, μ_y) is defined to be within the lesion, i.e., $(\mu_x, \mu_y) \in \mathcal{L}$ for all \mathcal{L} . In addition, the perimeter of the set \mathcal{L} must be one continuous closed contour.

In order to segment the potential lesion, the "validity" of various image partitions $\mathcal{L}_i; i = 1, \dots, T$ is evaluated. For conventional region growing segmentation, the partitions are typically defined as

$$\mathcal{L}_i^{(\text{rg})} = \{(x, y) : f(x, y) > t_i\} \quad (2)$$

where t_i is a gray-level threshold. This makes use of the fact that lesions tend to be brighter than the surrounding tissue but it does not directly take shape into account, i.e., irregular shapes can be evaluated. Shape is, however, typically indirectly analyzed in these methods when searching for the

partition to represent the segmented lesion [10], [11]. Fig. 1(b) shows an example of some of the irregular partitions that can arise in conventional region growing. The partitions are lesion-shaped at high thresholds, but tend to effuse into the background at lower thresholds, and are not representative of the lesion.

Conventional region growing defined the lesion partitions $\mathcal{L}_i^{(\text{rg})}$ based solely on gray-level information in the image. The new algorithms proposed in this paper add additional *a priori* information into the creation of the lesion partitions. Lesions tend to be compact, meaning that their shapes are typically convex. To incorporate this knowledge into the creation of the partitions, the original image is multiplied by a function, called the constraint function, that suppresses distant pixel values. For this study we chose to use an isotropic Gaussian function centered on the seed point location (μ_x, μ_y) with a fixed variance σ_c^2 as the constraint function. The function $h(x, y)$ resulting from the multiplication of the original ROI with the constraint function is given by

$$h(x, y) = f(x, y)N(x, y; \mu_x, \mu_y, \sigma_c^2) \quad (3)$$

where $N(x, y; \mu_x, \mu_y, \sigma_c^2)$ is a circular normal distribution [see Fig. 2(b)] centered at (μ_x, μ_y) with a variance σ_c^2 . Other constraint functions may be more appropriate for different

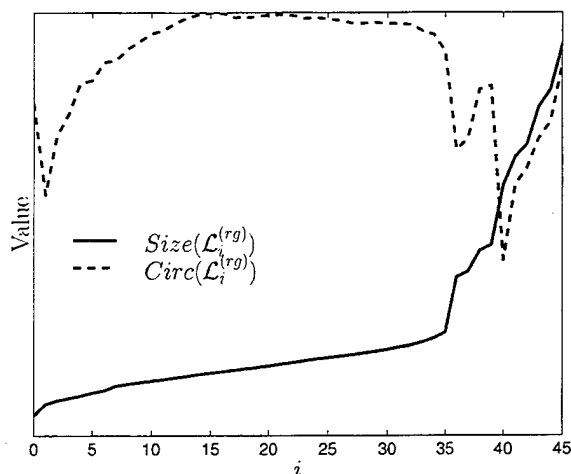


Fig. 3. Features employed in determining the final partition for conventional region growing. Here, i corresponds to the different gray-level intervals.

segmentation tasks. We have found, however, that a Gaussian works well for mammographic lesions. Fig. 2(c) shows an example of the function $h(x, y)$. At a given threshold, the partitions returned by thresholding are more compact than before because distant pixels are suppressed, i.e., a geometric constraint has been applied. The new partitions are defined as

$$\mathcal{L}_i = \{(x, y) : h(x, y) > t_i\}. \quad (4)$$

An example is shown in Fig. 1(c). Note that all of the partitions are now "lesion-like;" they are influenced by both the gray-level information and the geometric constraint. The value of the parameter σ_c^2 will be discussed later.

A. Region-Growing Segmentation

In conventional region growing, a feature or multiple features may be calculated for the partitions described in (2). For example, circularity $Circ()$ and size $Size()$ can be calculated for every $\mathcal{L}_i^{(rg)}$ as demonstrated in Fig. 3. The final partition is chosen by analyzing these functions and determining transition points or jumps in the features [4], [10], [11]. As Fig. 3 shows, the data can exhibit multiple transition points, and determining a jump by analyzing the first derivative of noisy data is difficult. If a transition point cannot be found, the segmentation algorithm fails to return a final partition.

B. Radial Gradient Segmentation

Given a series of partitions \mathcal{L}_i from (4), one must determine which of these partitions best delineates the lesion. One method is to apply a utility function. Bick *et al.* [12] employed a RGI utility function in his lesion segmentation algorithm that utilized Fourier descriptors to describe the shapes of lesions. We have employed the RGI measure on the image $f(x, y)$ around the margin of each partition \mathcal{L}_i as a utility function. For every partition \mathcal{L}_i the RGI is calculated (see Fig. 5), and the partition with the maximum RGI is returned as the final lesion partition. It is important to note that the partitions \mathcal{L}_i are generated using the processed image $h(x, y)$ while the RGI measure is computed on the original image $f(x, y)$.

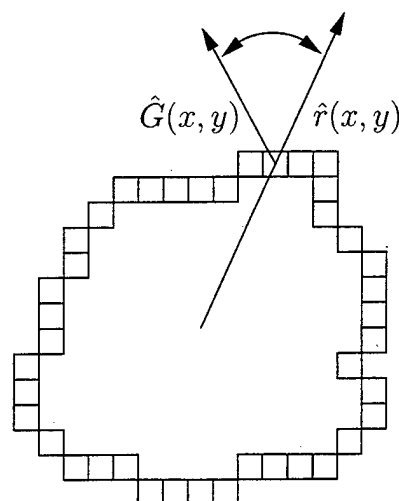


Fig. 4. The geometry used in calculating the RGI . The squares represent margin pixels \mathcal{M}_i of the partition \mathcal{L}_i being evaluated.

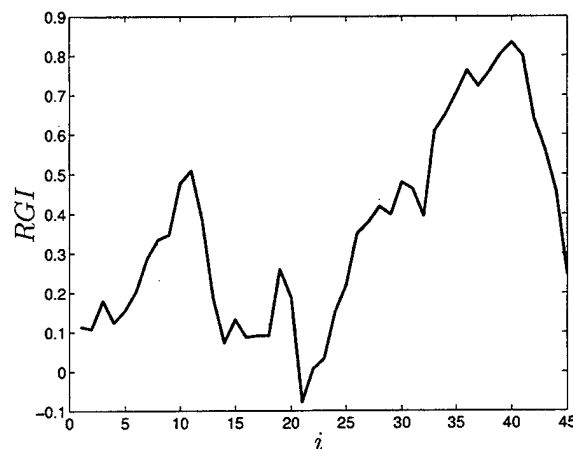


Fig. 5. The RGI as a function of the different partition \mathcal{L}_i for the image shown in Fig. 1(a). The partition with the largest RGI value is returned as the final lesion partition. Here, i corresponds to the different gray-level intervals.

The RGI is computed as follows. Given a partition \mathcal{L}_i (4) we can define the margin as

$$\mathcal{M}_i = \{(x, y) : (x, y) \in \mathcal{L}_i \text{ and either } (x-1, y), (x+1, y), (x, y+1), \text{ or } (x, y-1) \notin \mathcal{L}_i\}. \quad (5)$$

This states that a point is on the margin if it has at least one neighbor that is not in the lesion. The RGI is given by

$$RGI = \left(\sum_{(x,y) \in \mathcal{M}_i} \|\hat{G}(x, y)\| \right)^{-1} \sum_{(x,y) \in \mathcal{M}_i} \hat{G}(x, y) \frac{\hat{r}(x, y)}{\|\hat{r}(x, y)\|} \quad (6)$$

where $\hat{G}(x, y)$ is the gradient vector of $f(x, y)$ at position (x, y) and $(\hat{r}(x, y))/(\|\hat{r}(x, y)\|)$ is the normalized radial vector at the position (x, y) (Fig. 4). The RGI is a measure of the average proportion of the gradients directed radially outward. An RGI of one signifies that all the gradients around the margin are pointing directly outward along the radius vector and a -1

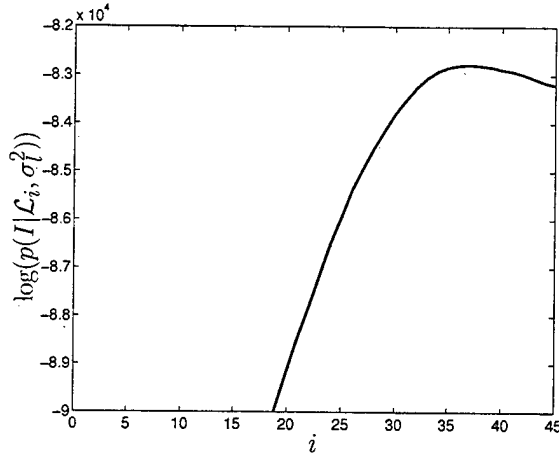


Fig. 6. A plot of the probability that the image occurred at different \mathcal{L}_i for the image shown in Fig. 1(a). The maximum-likelihood estimate of the partition is given by the partition which maximizes this function. Here, i corresponds to the different gray-level intervals.

indicates that all the gradients around the margin are pointing directly inward toward the center of the partition. The *RGI* value around the margin of a circular lesion, for example, is one. If, however, $f(x, y)$ is a uniform image, then the *RGI* value will be zero even if the margin \mathcal{M}_i is a circle.

C. Probabilistic Segmentation

The segmentation method based on probabilistic models is somewhat similar to the *RGI* method, except that the utility function is now a probability. The probability of pixel gray levels given a partition \mathcal{L}_i (4) is modeled as

$$p(f(x, y) | \mathcal{L}_i, \sigma_i^2) = \begin{cases} N(f(x, y); f(\mu_x, \mu_y), \sigma_i^2) & : (x, y) \in \mathcal{L}_i \\ z(f(x, y)) & : (x, y) \notin \mathcal{L}_i \end{cases} \quad (7)$$

where $N(f(x, y); f(\mu_x, \mu_y), \sigma_i^2)$ is a normal distribution centered at the seed point gray level $f(\mu_x, \mu_y)$, with a variance σ_i^2 , and $z(f(x, y))$ is a function to be described later. Lesions will not exhibit a large variation in pixel values, while the tissues surrounding the lesion may show large variation because they may consist of both fatty and dense regions. The uniformity of lesions is accounted for by a small-variance Gaussian function centered around the seed pixel value. The term $z(f(x, y))$ is a function that is estimated for each ROI using the gray levels from all of the pixels within the ROI although it is only employed in calculating $p(f(x, y) | \mathcal{L}_i, \sigma_i^2)$ for $(x, y) \notin \mathcal{L}_i$ [see (7)]. Finally, the probability of the image (or ROI) I given a partition \mathcal{L}_i is

$$p(I | \mathcal{L}_i, \sigma_i^2) = \prod_{(x, y) \in \mathcal{I}} p(f(x, y) | \mathcal{L}_i, \sigma_i^2). \quad (8)$$

The partition \mathcal{L}_i that is chosen is the one that maximizes the probability $p(I | \mathcal{L}_i, \sigma_i^2)$, i.e.,

$$p(I | \mathcal{L}_{\text{final}}, \sigma_i^2) = \underset{i}{\operatorname{argmax}} \{p(I | \mathcal{L}_i, \sigma_i^2)\}. \quad (9)$$

An example plot of $p(I | \mathcal{L}_i, \sigma_i^2)$ is shown in Fig. 6. Because there are a finite number of \mathcal{L}_i , we avoid the complexity of

an optimization problem choosing instead to evaluate all \mathcal{L}_i and determine the maximum.

The probability distribution for the gray levels when the pixels are outside the set \mathcal{L}_i is given by the function $z(f(x, y))$ [see (7)], which is estimated from all gray levels within the ROI. Kernel density estimation using an Epanechnikov kernel was employed to estimate this distribution [13]. The width of the kernel was optimally determined through cross validation [13]. Kernel density estimation is a method similar to histogram analysis except that a nonrectangular kernel is used to bin data and this kernel is swept across the function axis continuously. Histogram analysis, on the other hand, uses a box-function that is moved in increments of the box width. Figs. 9 and 10 show the calculated probability distributions for gray levels inside and outside \mathcal{L}_i for the ROI's shown in Figs. 7 and 8, respectively.

III. RESULTS

A. Parameter Estimation

The width σ_c^2 of the constraint function in (3) was determined based on knowledge of lesions and was not statistically determined. A value of 12.5^2 mm^2 was empirically determined to work well for our purposes. Larger lesions were also segmented with this value but spiculations and small deviations around the edge of the lesion were usually not delineated.

The parameter σ_l^2 in (7) is an unknown quantity and must be determined. The average variation of the gray levels within the radiologist's outlined truth for a screening, malignant database of 118 visible lesions was estimated. Fig. 11 shows the density distribution for these variations as measured by the standard deviation of the gray levels within the radiologist's outlines. A value of 0.038 was determined to be the most common standard deviation of pixel values within the radiologist's outlines. It is important to note that problems may arise when the radiographic presentation of lesions in other databases are substantially different from those in the database employed in this study. We, however, employed a database of 60 malignant, nonpalpable lesions obtained from roughly 700 needle biopsies performed during the years 1987 to 1993 and, thus, should be representative of the actual distribution.

The value of σ_l^2 can also be determined for each lesion individually. Instead of just using the most probable *a priori* value of σ_l^2 (as discussed above) one can apply Bayes' theorem to find that

$$p(\sigma_l^2 | I, \mathcal{L}_i) = \frac{p(I | \mathcal{L}_i, \sigma_l^2)p(\sigma_l^2 | \mathcal{L}_i)}{p(I | \mathcal{L}_i)} \quad (10)$$

where $p(I | \mathcal{L}_i, \sigma_l^2)$ is given by (8). If we assume that σ_l^2 and \mathcal{L}_i are independent, then $p(\sigma_l^2 | \mathcal{L}_i) = p(\sigma_l^2)$. The distribution of $p(\sigma_l^2)$ can be obtained from Fig. 11. Finally, we know that $p(I | \mathcal{L}_i) = \int d\sigma_l p(I | \mathcal{L}_i, \sigma_l^2)p(\sigma_l^2)$ which results in

$$p(\sigma_l^2 | I, \mathcal{L}_i) = \frac{p(I | \mathcal{L}_i, \sigma_l^2)p(\sigma_l^2)}{\int d\sigma_l p(I | \mathcal{L}_i, \sigma_l^2)p(\sigma_l^2)}. \quad (11)$$

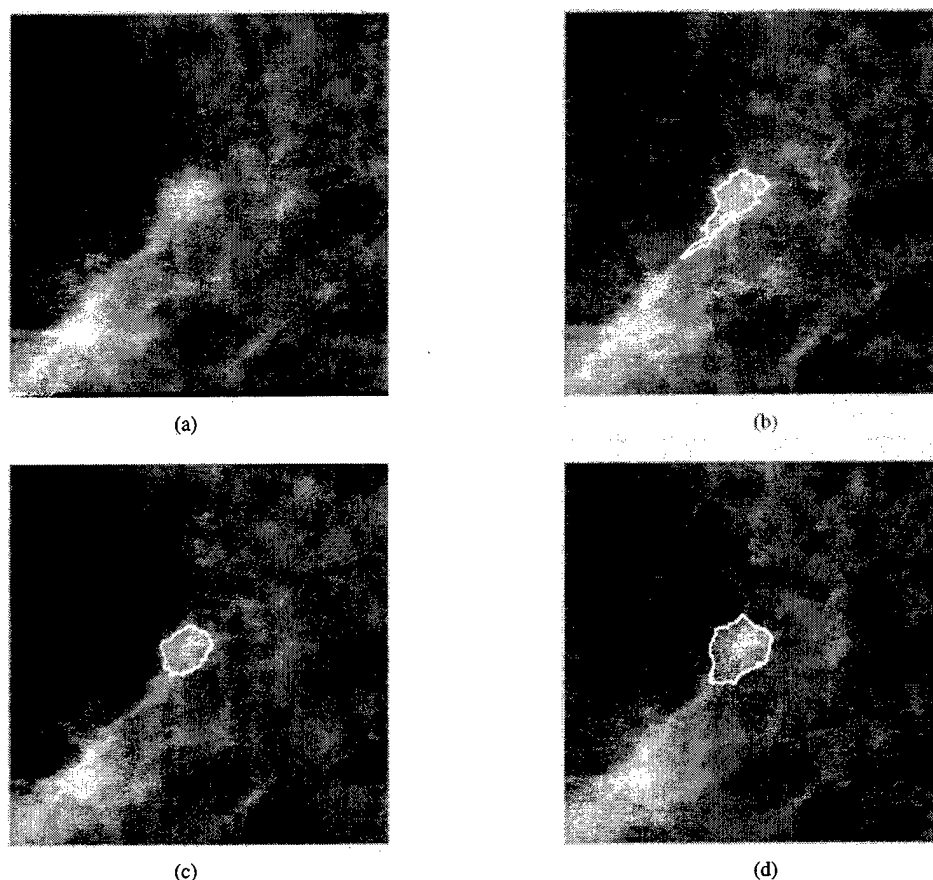


Fig. 7. Segmentation results for (a) a high-contrast lesion using (b) region growing, (c) *RGI*-based segmentation, and (d) probabilistic segmentation.

The probability of various values of σ_l^2 could be compared against each other and the optimal σ_l^2 estimated. Unfortunately, to estimate $p(\sigma_l^2 | I, \mathcal{L}_i)$ one must compute

$$\int d\sigma_l p(I | \mathcal{L}_i, \sigma_l^2) p(\sigma_l^2) \quad (12)$$

which involves integrating over all possible values of σ_l and is very time consuming. Not only do we have the problem of integrating over all σ_l values but the value computed is the probability given a partition \mathcal{L}_i . This leaves us with a dual optimization task. For a given σ_l^2 the optimal partition $\mathcal{L}_{\text{final}}$ is determined. This partition is then employed to determine a new optimal σ_l^2 . This process continues until there is convergence. For this research, we instead employed a constant value, i.e., the most probable *a priori* value of σ_l^2 .

B. Segmentation Performance

Segmentation results for a relatively simple (high contrast) lesion are shown in Fig. 7. All three methods, region growing, *RGI*-based segmentation, and probabilistic segmentation, perform well on this lesion. Region growing has somewhat undergrown the lesion and has a long tail. The *RGI*-based method and the probabilistic method segment the lesion better than region growing. Similar images are shown for a more difficult lesion on a border between a fatty region and the pectoralis muscle (Fig. 8). Because of the brightness of the

pectoralis muscle, region growing effuses into the background too soon and thus, the transition point found results in a grossly undergrown lesion. There are also vessels that can be radiographically seen passing through the center of this lesion. The *RGI*-based segmentation algorithm chooses the boundary of a vessel as the best partition because the *RGI* value around the vessel is larger than that around the actual lesion. The probabilistic segmentation algorithm, however, does not get confused by the vessel inside the lesion and correctly segments this difficult lesion.

In order to quantify the performance differences between the three different segmentation methods, the segmentation results were compared against radiologists' outlines of the lesions. The screening database of nonpalpable, biopsy-proven, malignant cancers with a total of 118 visible lesion ROI's was employed. For each lesion the seed point was calculated from the center of mass of the radiologist's outline. Once the lesion was segmented, an overlap measure O was calculated using the set returned from the segmentation algorithm \mathcal{L} and the radiologist's hand-drawn segmentation set \mathcal{T} . The overlap O is defined as the intersection over the union, i.e.,

$$O = \frac{\text{Area}(\mathcal{L} \cap \mathcal{T})}{\text{Area}(\mathcal{L} \cup \mathcal{T})}. \quad (13)$$

The value of O is bound between zero (no overlap) and one (exact overlap). A threshold needs to be set in order to classify a result as an "adequate" segmentation, i.e., if O is greater than

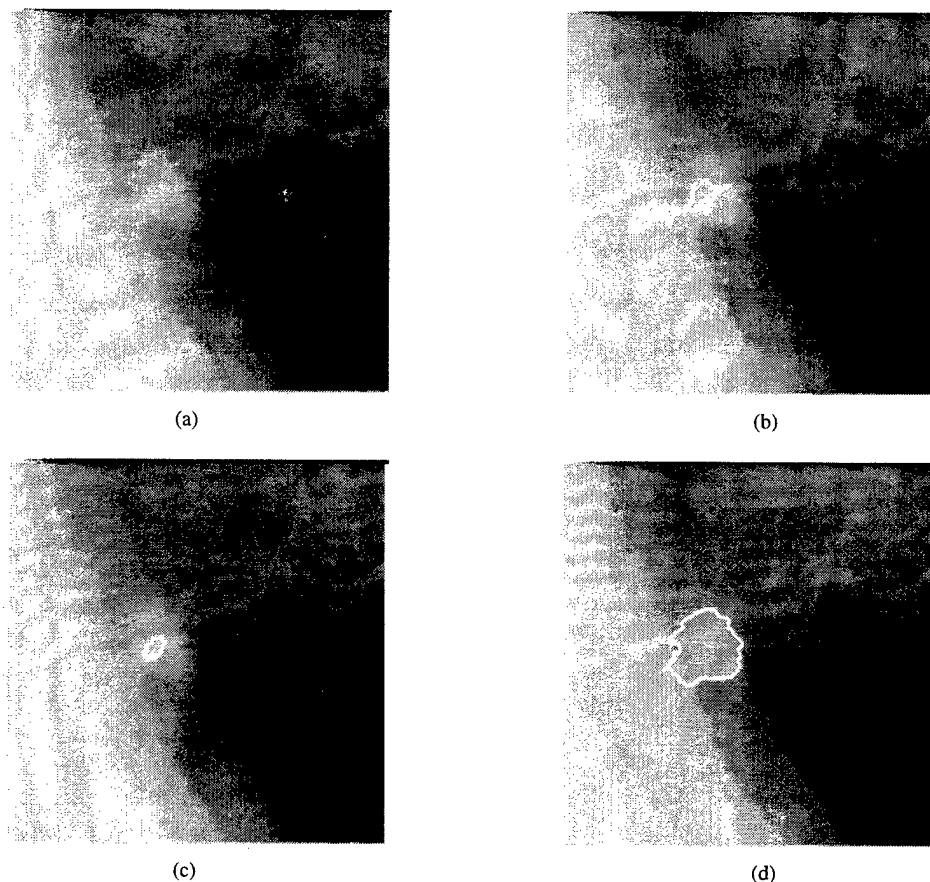


Fig. 8. (a) Segmentation results for a lesion on the boundary between a fatty area and the pectoralis muscle using (b) region growing segmentation, (c) *RGI*-based segmentation, and (d) probabilistic segmentation.

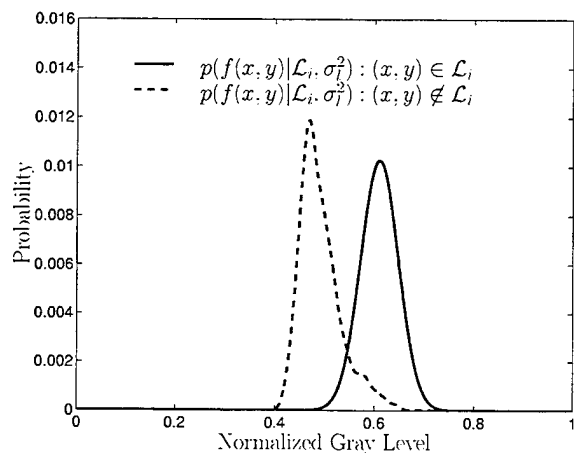


Fig. 9. Probability distributions employed when a pixel is inside or outside of the set in question for the image shown in Fig. 7. The distribution employed when $(x, y) \in \mathcal{L}_i$ is a Gaussian centered at the seed point gray level with a variance of σ_i^2 . The distribution $z(f(x, y))$ is employed when $(x, y) \notin \mathcal{L}_i$ and is estimated from all gray values within the ROI.

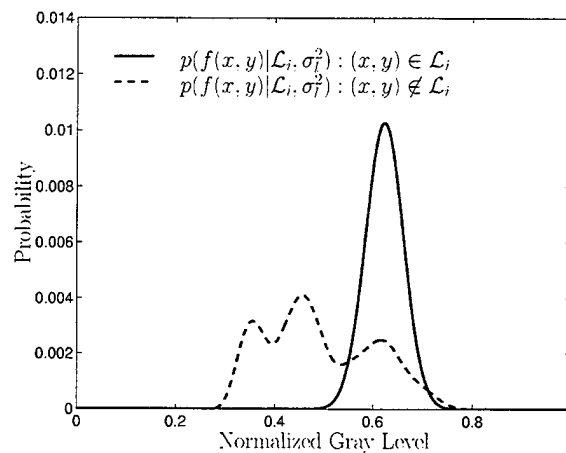


Fig. 10. Probability distributions employed when a pixel is inside or outside of the set in question for the ROI shown in Fig. 8. The distribution employed when $(x, y) \in \mathcal{L}_i$ is a Gaussian centered at the seed point gray level with a variance of σ_i^2 . The distribution $z(f(x, y))$ is employed when $(x, y) \notin \mathcal{L}_i$ and is estimated from all gray values within the ROI.

a certain value then the lesion is considered to be correctly segmented.

Fig. 12 shows a plot of the fraction of lesions correctly segmented at various overlap threshold levels. The probabilistic segmentation algorithm outperformed the other methods. Also shown in Fig. 12 is the performance of a different radiologist

in extracting the lesions as compared with the first radiologist. It is interesting to note that the performances of the *RGI*-based and probabilistic methods are not too dissimilar from the human performance. Region growing never yielded all lesions correctly segmented even when the overlap threshold was zero because the method failed to find a transition point in many of the images.

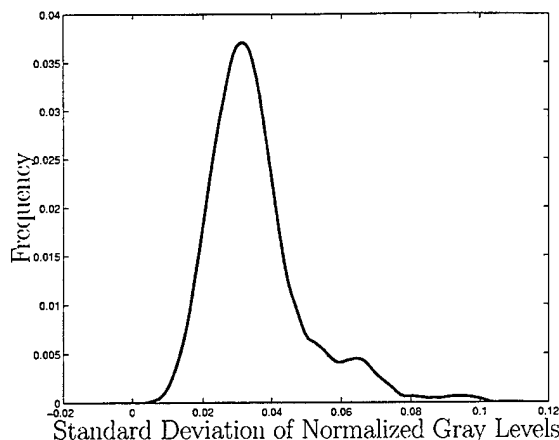


Fig. 11. The distribution of standard deviations of the gray levels within the radiologist's outlined lesions for a database of 60 malignant lesions (118 ROI's). The pixel values of the images were normalized to be between zero and one.

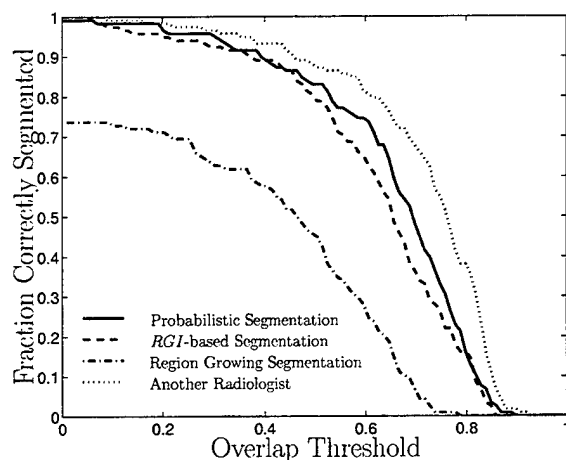


Fig. 12. The performance of the different segmentation methods on a database of malignant lesions as compared with a radiologist's outlines. Also shown is the agreement of another radiologist's outlines of the lesions in the databases with the outlines of the first radiologist.

IV. DISCUSSION

Bayesian analysis could be applied to the probabilistic segmentation algorithm resulting in

$$p(\mathcal{L}_i | I, \sigma_i^2) = \frac{p(I | \mathcal{L}_i, \sigma_i^2)p(\mathcal{L}_i)}{p(I)}. \quad (14)$$

By analyzing (14) one finds that the $p(\mathcal{L}_i)$ is a term that penalizes partitions which are not "lesion" shaped. The partitions in our study, however, are obtained after the shape constraint function (4) has been applied so every partition analyzed is "lesion" shaped and thus, a Bayesian analysis is not necessary. If deformable contours are employed instead of a series of lesion-shaped partitions, then Bayes' rule (14) should be applied.

The assumption throughout this paper has been that appropriate partitions can be generated by gray-level thresholding the function $h(x, y)$ (3). This assumption, as is shown by the results of this paper, is generally appropriate for most

lesions. There are, however, cases where thresholding $h(x, y)$ does not generate adequate partitions for a given lesion. In some cases, oddly shaped lesions may be surrounded by glandular structures which may confuse the algorithm into calling those normal structures part of the lesion. Spiculations, which are common in malignant lesions, are, in general, not included in the final lesion partition because of the application of the constraint function. The purpose of the segmentation algorithms described in this paper, however, is to determine the general shape of the lesions and not necessarily the detailed shape in which all spiculations are demarcated.

There is an implicit model that arises from the density functions employed in the probabilistic segmentation algorithm. Equation (7) assumes that all pixels within the lesion come from a Gaussian distribution centered at the seed point pixel value. The lesion model from which this distribution arises is a very simple one: a lesion has uniform gray levels with fluctuations arising from both noise and structure. In the future, more complex models, such as modeling a lesion as a projection of a sphere, can be implemented. The distributions, however, become more difficult with which to work and the assumption of independence in (8) and (10) is no longer valid.

Different initial seed points will result in different segmentation results. For both the *RGI*-based and probabilistic segmentation algorithms, the results are very similar given small changes in the seed point location. If, however, the seed point is selected to be at the very edge of the lesion, then the final partitions returned by both the *RGI*-based and probabilistic algorithms will be poor.

We comparatively evaluated the three segmentation methods at various overlap criteria (Fig. 12) because different investigators may use different evaluation criteria as well as different databases. Previously, we have shown that the reported performance of a computer detection method can greatly vary depending on the criteria used in tabulating sensitivity and specificity [14].

The performance differences between the probabilistic algorithm and the *RGI*-based method are small. Both, however, substantially outperform conventional region growing. It is expected that this better segmentation performance will, in the future, result in more meaningful features being extracted from potential lesion regions, and, ultimately, in better classification of malignant lesions from normal tissue regions.

V. CONCLUSION

We have developed two new methods of seeded lesion segmentation for use in digital mammography. These new methods substantially outperform conventional region growing segmentation. At an overlap threshold of 0.3, region growing correctly identified 62% of the lesions in our database, while the *RGI*-based and probabilistic segmentation methods correctly segmented 92% and 96% of the lesions, respectively. With these new segmentation results we hope to find and extract new features that will help differentiate between actual lesions and false detections, thus improving the overall performance of computerized mass detection.

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Automated Computerized Classification of Malignant and Benign Masses on Digitized Mammograms¹

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Rationale and Objectives. To develop a method for differentiating malignant from benign masses in which a computer automatically extracts lesion features and merges them into an estimated likelihood of malignancy.

Materials and Methods. Ninety-five mammograms depicting masses in 65 patients were digitized. Various features related to the margin and density of each mass were extracted automatically from the neighborhoods of the computer-identified mass regions. Selected features were merged into an estimated likelihood of malignancy by using three different automated classifiers. The performance of the three classifiers in distinguishing between benign and malignant masses was evaluated by receiver operating characteristic analysis and compared with the performance of an experienced mammographer and that of five less experienced mammographers.

Results. Our computer classification scheme yielded an area under the receiver operating characteristic curve (A_z) value of 0.94, which was similar to that for an experienced mammographer ($A_z = 0.91$) and was statistically significantly higher than the average performance of the radiologists with less mammographic experience ($A_z = 0.81$) ($P = .013$). With the database used, the computer scheme achieved, at 100% sensitivity, a positive predictive value of 83%, which was 12% higher than that for the performance of the experienced mammographer and 21% higher than that for the average performance of the less experienced mammographers ($P < .0001$).

Conclusion. Automated computerized classification schemes may be useful in helping radiologists distinguish between benign and malignant masses and thus reducing the number of unnecessary biopsies.

Key Words. Breast, biopsy; breast neoplasms, diagnosis; computers, diagnostic aid; computers, neural network.

The present widespread use of mammography for early detection of breast cancer in asymptomatic women increases the importance of radiologists recognizing the mammographic features that distinguish carcinomas from benign abnormalities. Despite improvements in the criteria used to differentiate benign from malignant lesions of the breast (1–6), considerable misclassification of lesions occurs in everyday clinical practice. At many centers, only 15%–30% of mammographically detected lesions analyzed by means of surgical breast biopsy are actually malignant (7,8). There also is great variation (7%–40%) in positive biopsy rates among individual radiologists (9).

Computer-aided diagnosis in mammography can be defined as a diagnosis made by a radiologist who takes into account the output from a computer analysis of a mammogram. Many investigators have studied the use of computer analysis as an aid in the early detection of breast cancer (10–13). The development of computer aids that help in the classification portion of a mammographic work-up also has been studied. An objective computer classification scheme capable of differentiating between benign and malignant masses at a level similar to that of

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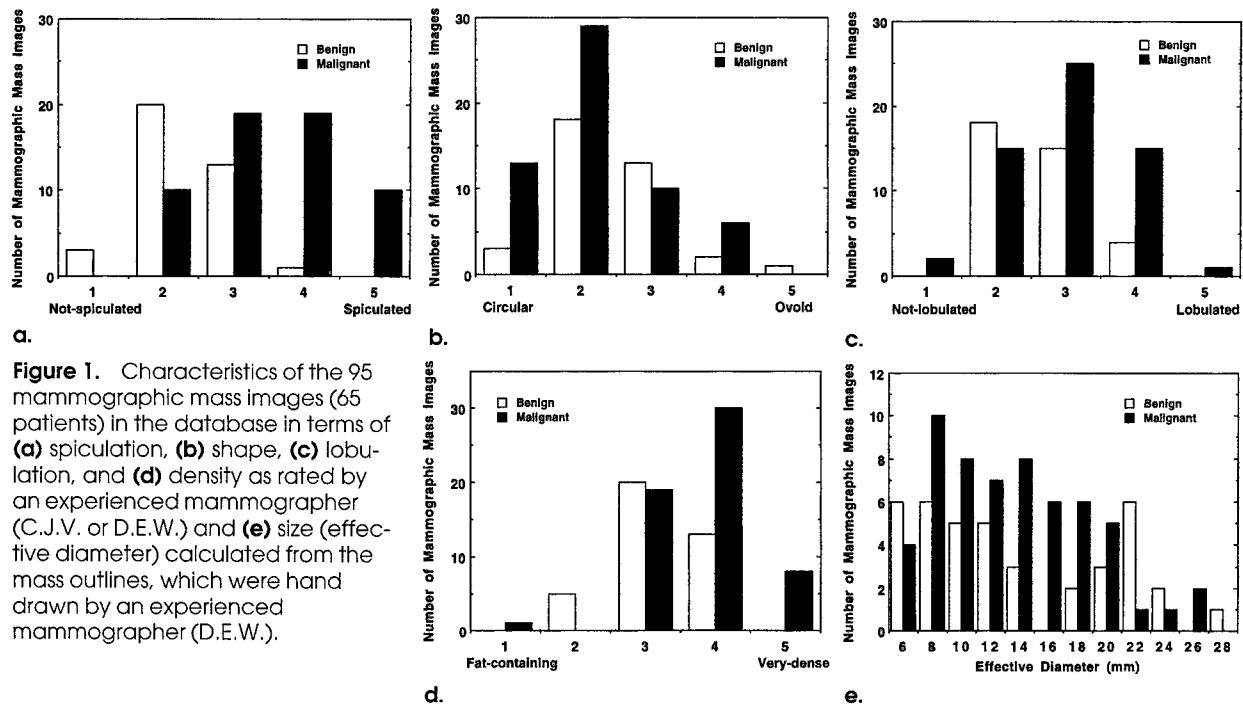


Figure 1. Characteristics of the 95 mammographic mass images (65 patients) in the database in terms of (a) spiculation, (b) shape, (c) lobulation, and (d) density as rated by an experienced mammographer (C.J.V. or D.E.W.) and (e) size (effective diameter) calculated from the mass outlines, which were hand drawn by an experienced mammographer (D.E.W.).

experienced mammographers would help radiologists improve accuracy, decrease variability, and reduce the number of unnecessary biopsies.

In the classification of lesions, investigators have taken advantage of the ability of radiologists to extract features related to the margin and density of mammographic abnormalities and have used computers to merge these (human-extracted) features into diagnoses (14–18). Use of computer-based decision systems such as rule-based methods, discriminant analysis, and artificial neural networks (ANNs) to merge the information extracted by either human observers or computers has been investigated (14–19). In addition, computerized techniques can be used to automatically extract individual image features such as spiculation (20–22), margin sharpness (23), irregularity (24), and density (25). Some investigators have attempted to use multiple computer-extracted features to classify masses (24,26).

In this study, we address the classification task in mammographic work-up and introduce a set of morphologic features similar to the ones used by practicing radiologists to characterize margin and density of a mass. We then merge these features with a spiculation measure into an estimated likelihood of malignancy for individual lesions. It should be noted that our fully automated computerized method includes automated lesion segmentation, automated feature extraction, and automated classification. The

effectiveness of each individual feature and the role of each feature in classification of masses were studied.

To process the computer-extracted features more effectively, a two-step rule-based method and an ANN were used to merge these features. To overcome the limitations of these two individual types of classifiers for this particular task, integration of a rule-based method and an ANN was introduced as a hybrid information-processing approach. The hybrid system provides more power as a computer-based classifier by allowing emulation of humans in their information-processing and decision-making capabilities. The ability of the three classifiers to merge the computer-extracted features into a correct diagnosis was evaluated in 65 patients by using receiver operating characteristic (ROC) analysis (27,28). The performance of the computer was compared with that of an experienced mammographer and five radiologists with less mammographic experience.

MATERIALS AND METHODS

The database used in this study consisted of 95 clinical mammographic images (Min-R screen/OM-1 film; Eastman Kodak, Rochester, NY), each of which contained a mass. Thirty-eight of the images showed benign lesions, and 57 showed malignant lesions. The 95 mammograms were collected from examinations of 65 patients and repre-

sented an entire database gathered in our laboratory from December 1985 to October 1989. Twenty-six of the 65 patients had benign breast abnormalities, and 39 patients had breast cancer. Both mediolateral oblique and craniocaudal views were available for 30 of the patients (12 of 26 patients with benign lesions and 18 of 39 patients with malignant lesions). According to the original selection criteria, patients were chosen who had masses that were difficult to classify and who had undergone open biopsy or long-term mammographic follow-up. All but one patient underwent biopsy for the suspicion of breast cancer, and in the remaining one patient the disease was deemed benign on the basis of follow-up of more than 5 years. The screen-film mammograms were digitized with an optical drum scanner (FIP II; Fuji Film, Tokyo, Japan) at a sampling distance of 0.1 mm and 10-bit quantization.

To characterize the database, two experienced mammographers (C.J.V., D.E.W.) rated each mass with respect to spiculation, lobulation, shape, and density by using a five-point scale in which 1 corresponded to not spiculated, not lobulated, circular, or fat containing and 5 corresponded to definitely spiculated, lobulated, ovoid, or very dense, respectively. These distributions are shown in Figure 1a–1d. The size of each mass in terms of effective diameter was also estimated based on the region outlined on the computer by an experienced mammographer (D.E.W.). The effective diameter of a mass is defined as the diameter of the equivalent circle (whose area is the same as the area of the grown region) of the identified mass region (29). The distribution of size in terms of effective diameter for the masses depicted on the 95 images is shown in Figure 1e; the average size was approximately 1.3 cm.

Our current classification scheme consists of three stages: (a) automated segmentation of mammographic masses from surrounding parenchyma, (b) automated feature extraction, and (c) automated classification, which yields an estimation of malignancy of a mass by means of one of three classifiers—a rule-based method, an ANN, or a hybrid system (ie, a combination of a one-step rule-based method and an ANN).

The area under the ROC curve (A_z) was used to evaluate the ability of our computer classification scheme to utilize the three different classifiers to differentiate benign from malignant masses. Clinically, the specificities at high sensitivity levels are most relevant because the “cost” of missing a cancer is greater than the cost of performing a biopsy to assess a benign lesion. Thus, the average performances in a high sensitivity range (true-posi-

tive fraction [TPF_0] above 0.90) were evaluated for both our classification schemes and the observers by using a partial area index, $_{TPF}A_z'$, from 0 to 1, which is the portion of the A_z that lies above a preselected sensitivity threshold (TPF_0) in a conventional ROC graph divided by the constant $(1 - TPF_0)$ (30). These performances, in terms of specificity at a given sensitivity level, were also evaluated. In this study, we chose to calculate specificity at a sensitivity level of 100% because the aim of creating the computer output in our research was to aid radiologists in reducing the number of unnecessary biopsies performed without misclassifying any cancers.

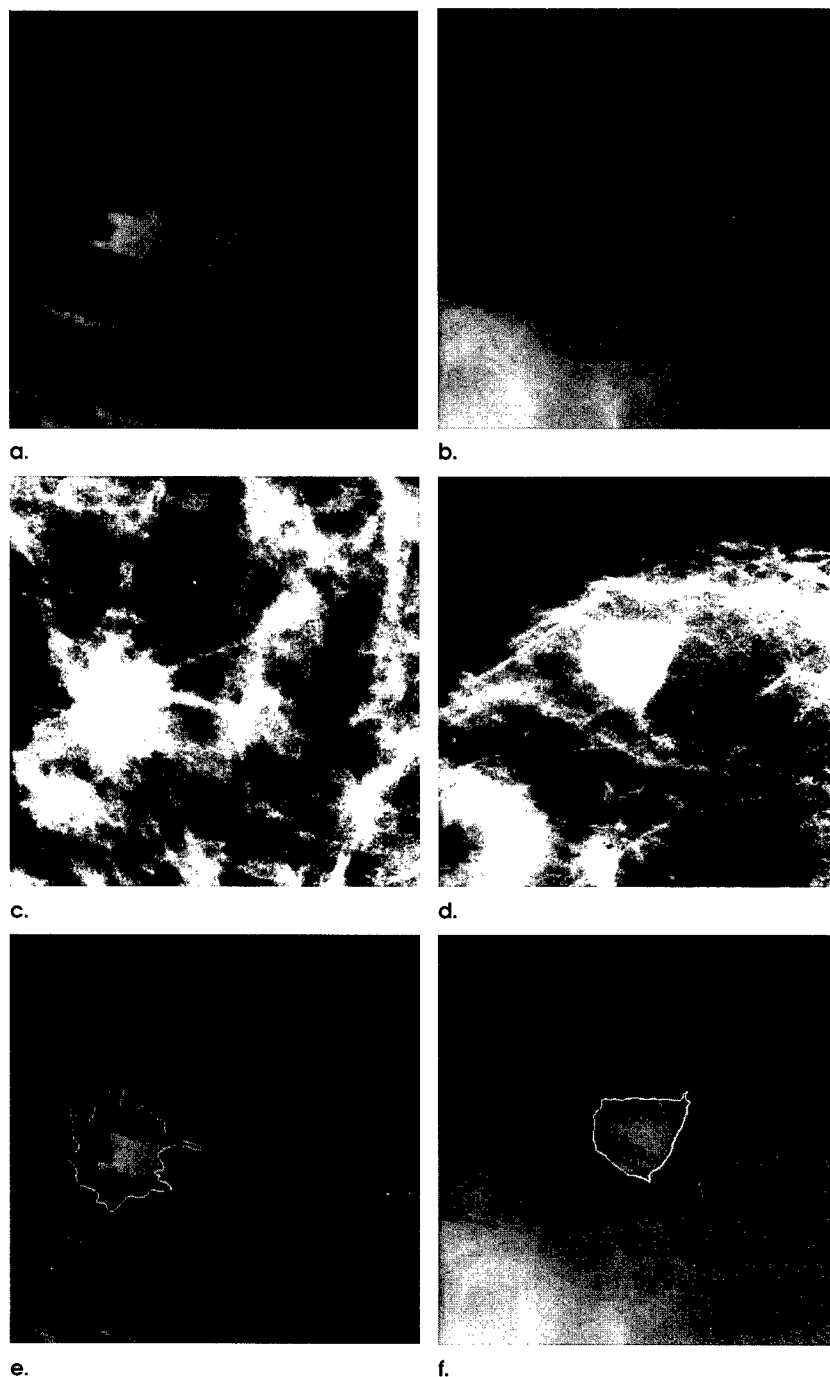
Segmentation

Segmentation of a mass from the background parenchyma was accomplished by using a multiple-transition-point, gray-level, region-growing technique (22). Segmentation begins within a 512×512 -pixel region of interest manually centered about the abnormality in question, as illustrated in Figure 2a and 2b. In clinical practice, the location of the mass could be identified either by a radiologist or with a computer-detection scheme (31) and then fed into the classification scheme for an output in regard to the likelihood of malignancy. To correct for the nonuniformity of the background distribution and to enhance image contrast for better segmentation of masses, background trend-correction and histogram-equalization techniques were applied to the 512×512 -pixel region of interest (22). The corresponding enhanced images of the malignant and benign masses are shown in Figure 2c and 2d, respectively. The computer-identified margins of the malignant and benign masses are superimposed on the images of the original masses in Figure 2e and 2f. For comparison, margins of the same images hand drawn by an experienced mammographer are shown in Figure 2g and 2h.

Computer-extracted Radiographic Features: Margin and Density

The margin, shape, and density of a mass are three major characteristics used by radiologists in classifying masses. Different characteristics of these features are associated with different levels of probability of malignancy (4,6,32). To determine the likelihood of malignancy associated with different margin and density characteristics, we developed algorithms that extract two features that characterize the margin of a mass (spiculation, sharpness) and three features that characterize the density of a mass (average gray level, contrast, texture).

Figure 2. Mammographic images of (a) a malignant mass and (b) a benign mass in a 512×512 -pixel region of interest; enhanced images of the (c) malignant and (d) benign masses after image processing; and computer-extracted margins superimposed on the (e) malignant and (f) benign masses (Fig 2 continues).



We did not explicitly devise a specific measure to characterize the shape of a mass for the purpose of classification, but measures related to shape are embedded within the other measures.

Margin.—Margin characteristics are very important in differentiating between benign and malignant masses. To determine the likelihood of malignancy of a mass based on its margin, two major margin characteristics—spicula-

tion and sharpness—were measured. Margin spiculation is the most important indicator for malignancy, with spiculated lesions having a greater than 90% probability of malignancy (6). Margin sharpness is also very important in determining whether a mass is benign or malignant; an ill-defined margin indicates possible malignancy, and a well-defined margin indicates likely benignity. Only about 2% of well-defined masses are malignant (2).

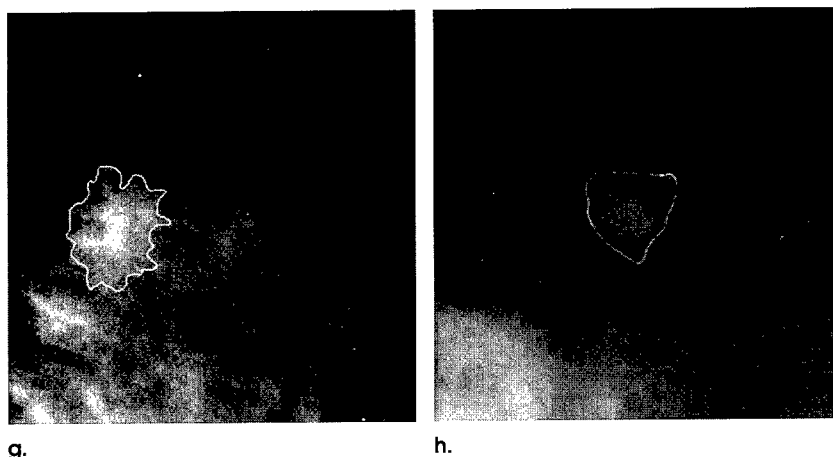


Figure 2 (continued). An experienced mammographer's hand-drawn margins of the (g) malignant and (h) benign masses.

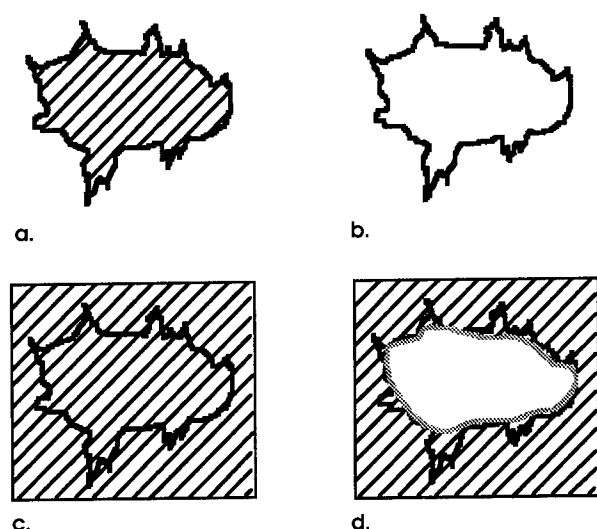


Figure 3. Illustration of the four neighborhoods used for feature extraction: (a) grown region, (b) margin, (c) encompassing region, and (d) surrounding periphery (cross-hatched region).

The spiculation measure is determined from an analysis of radial edge gradients (22). The spiculation measure evaluates the average angle (in degrees) by which the direction of the maximum gradient at each point along the margin of a mass deviates from the radial direction, the direction pointing from the geometric center of the mass to the point on the margin. The actual measure is the full width at half maximum (FWHM) of the normalized edge-gradient distribution calculated for a neighborhood of the grown region of the mass with respect to the radial direction (22). This measure is able to quantify the degree of spiculation of a mass primarily because the direction of maximum gradient along the margin of a spiculated mass

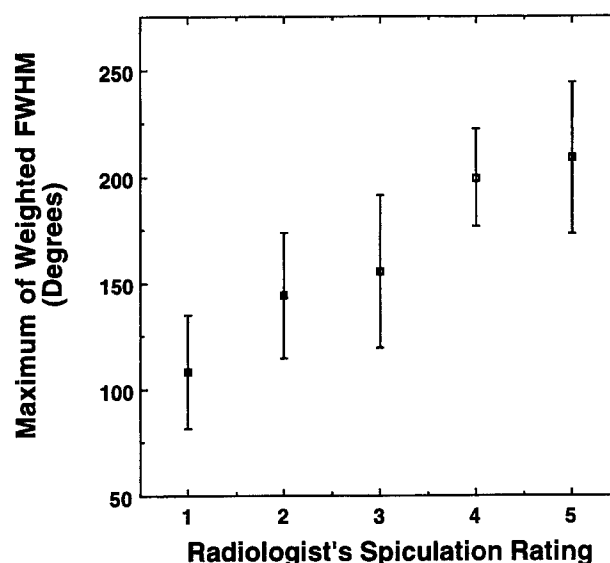


Figure 4. Correlation of the spiculation measure (weighted FWHM, in degrees) with the spiculation ratings (Fig 1a) of an experienced mammographer for a database of 95 mass images. The error bars indicate the variation in the spiculation measure for each spiculation rating given by the radiologist.

varies greatly from its radial direction, whereas the direction of the maximum gradient along the margin of a smooth mass is similar to its radial direction. The spiculation measure was extracted not only along and within the margin of a mass (Fig 3a, 3b) but also in enlarged neighborhoods of the computer-identified mass region as shown in Figure 3c and 3d. In this way, potentially more subtle spicules that are difficult to delineate by region growing could be better extracted. The two enlarged neighborhoods included 20 additional pixels around the computer-identified mass region. A neighborhood of this size is large enough to accommodate thin or short spicules radiating from the margin of a mass.

To maximize the sensitivity of the spiculation measure, all the possible signs of spiculation identified from the four neighborhoods were considered; the greatest value of the FWHM measures from the four neighborhoods was used to indicate the spiculation of a mass. However, because of differences in the ability of FWHM measures from the four neighborhoods to capture spiculation information (22), the FWHM measures were weighted differently. The weighting factor used for the two enlarged neighborhoods was 1.0, and that used for the other two neighborhoods was 0.85. This weighted spiculation measure correlates well with an experienced mammographer's spiculation rating ($r = .64$; $P < .0001$) (Fig 4). In addition, the level of performance of the spiculation measure ($A_z = 0.88$) was similar to that of the experienced mammographer's spiculation ratings ($A_z = 0.85$) in terms of the ability to distinguish between benign and malignant masses based solely on spiculation (22).

The sharpness of the margin of a mass can be described as well defined, partially ill defined, or ill defined. The average margin sharpness can be quantified by calculating the magnitude of the average gradient along the

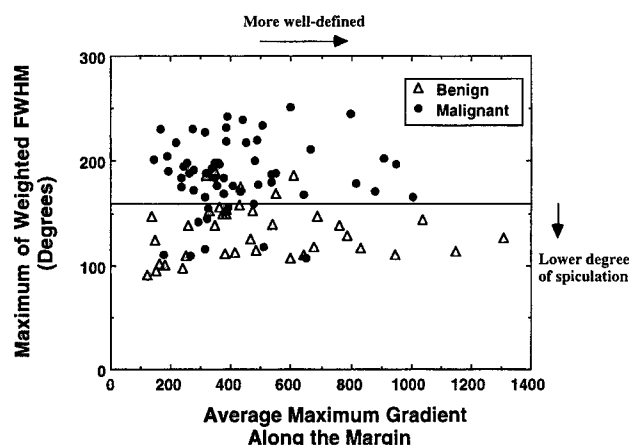


Figure 5. Cluster plot of the spiculation measure (weighted FWHM) versus the margin sharpness measure (average gradient) along the margin for 95 mass images. The horizontally drawn line indicates the cutoff on the FWHM measure chosen to distinguish between spiculated and nonspiculated masses.

Figure 6. Examples of masses with (a) a spiculated margin, (b) an ill-defined margin, (c) a partially ill-defined margin, and (d) a well-defined margin shown by mammography.

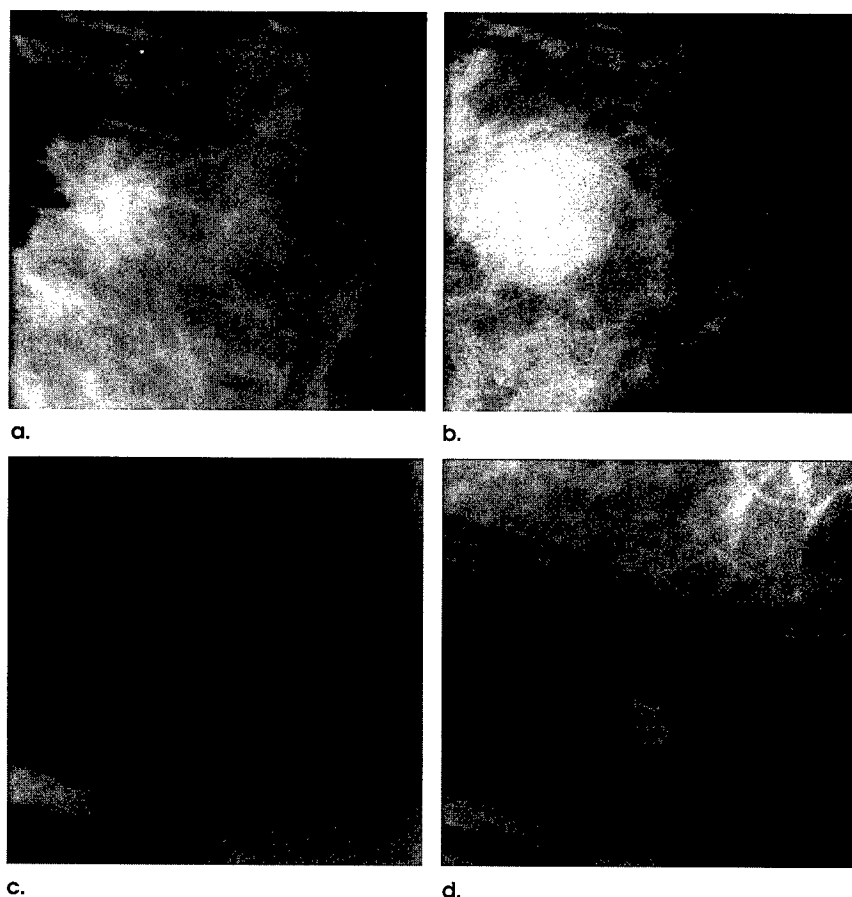


Table 1
Examples of Spiculation and Margin-Sharpness Measures for Four Selected Masses

Mass Type	Radiologist's Spiculation Rating	FWHM Measure	Average Gradient Along the Margin
Spiculated	5	240	513
Ill defined/obscured	3	118	318
Partially ill defined/obscured	3	111	962
Well defined	2	111	1,315
Maximum value in the database	5	242	1,315
Minimum value in the database	1	88	127

margin of the mass. A well-defined margin has a large value for the average margin sharpness measure, whereas an ill-defined margin has a small value.

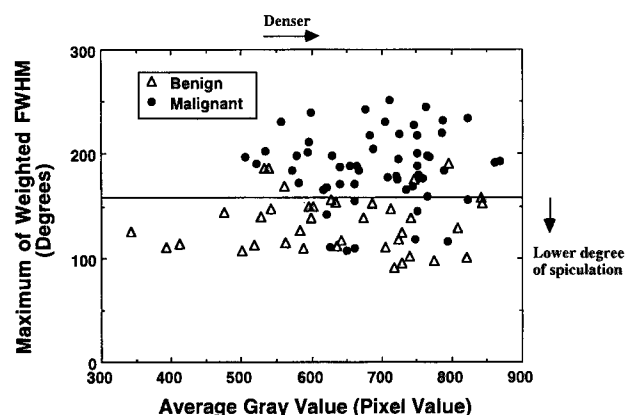
Figure 5 shows the relationship between the two margin measures for the 95 mass images. The horizontally drawn line indicates a cutoff on the FWHM measure used to categorize spiculated masses and nonspiculated masses. It should be noted that there is much more overlap between benign and malignant masses in terms of margin sharpness than in terms of margin spiculation. With the threshold of 160° for the spiculation measure, most of the malignant masses were in the spiculated category ($\text{FWHM} > 160^\circ$). At this threshold, five of 39 malignant masses and 22 of 26 benign masses were classified as nonspiculated. In addition, in the nonspiculated category, masses with a higher value for the margin-sharpness measure tended to be benign. This finding is in agreement with radiologists' visual perception in determining the benign versus malignant nature of masses. Thus, to determine the likelihood of malignancy of a mass based on the two margin characteristics described, it is more effective to use first the spiculation measure to identify spiculated masses (which are very likely to be malignant) and to determine their likelihood of malignancy based on their degree of spiculation. The margin-sharpness measure can then be used further to determine the likelihood of malignancy of the remaining (ie, nonspiculated) masses.

Figure 6 shows examples of masses with spiculated, ill-defined, partially ill-defined, and well-defined margins. The calculated spiculation and margin-sharpness measures for these four masses are listed in Table 1. The spiculated mass (radiologist's spiculation rating of 5) had a FWHM measure of 240° in a database with a maximum degree of spiculation of 242° and a minimum of 88° . This mass was correctly identified as highly spiculated and thus was not further analyzed with the margin-sharpness measure. The three smoother masses, each with spiculation ratings by the

radiologist of 2 or 3, had similar spiculation measures that ranged from 111° to 118° . They were classified as nonspiculated masses ($\text{FWHM} < 160^\circ$) and were further evaluated with the margin-sharpness measure. The margin-sharpness measures of the three masses were well separated, with the well-defined margin having the highest value (sharpness of 1,315), the partially ill-defined margin having the second highest value (sharpness of 962), and the ill-defined margin having the lowest value (sharpness of 318) in a database with margin-sharpness measures that ranged from 127 to 1,315. This illustrates the usefulness of the margin-sharpness measure in further discriminating between masses in the nonspiculated category.

Density.—Although the radiographic density of a mass may not by itself be as powerful a predictor as the margin features in distinguishing between benign and malignant masses, taken with these features density assessment can be extremely useful (4). The evaluation of the density of a mass is of particular importance in diagnosing circumscribed, lobulated, indistinct, or obscured masses (4) that are not spiculated.

To assess the density of a mass radiographically, we introduced three density-related measures (average gray level, contrast, texture) that characterize different aspects of the density of a mass. These measures are similar to those used intuitively by radiologists. Average gray level is obtained by averaging the gray-level values of each point within the grown region of a mass. Contrast is the difference between the average gray level of the grown mass and the average gray level of the surrounding fatty areas (areas with gray-level values in the lower 20% of the histogram for the total surrounding area). Texture is defined here as the standard deviation of the average gradient within a mass, and it is used to quantify patterns that arise from veins, trabeculae, and other structures that may be visible through a low-density mass but not through a high-density mass. A mass of low radiographic



a.

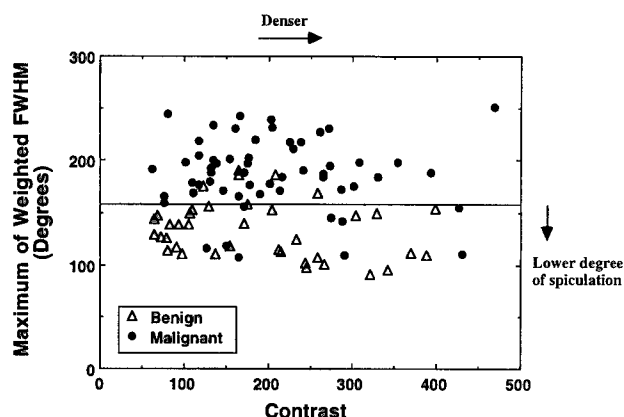
Figure 7. Cluster plots of the FWHM measure versus various secondary features: (a) average gray value of the extracted mass, (b) gray-value difference between a mass and its surrounding "fatty area," and (c) texture measure. The horizontally drawn line indicates the selected threshold for the FWHM measure that maximally separated spiculated from nonspiculated masses.

density should have low values for average gray level and contrast and a high value for texture, whereas a mass of high radiographic density should have high values for average gray level and contrast and a low value for texture.

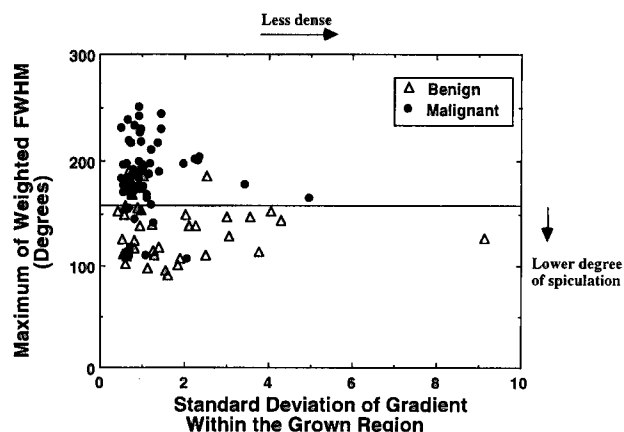
The relationships of the three density measures and the spiculation measure for the 95 mass images are shown in Figure 7. The drawn line indicates a cutoff, based on the spiculation measure (FWHM of 160°), that categorizes spiculated and nonspiculated masses. As can be seen from these cluster plots, the distribution of benign and malignant nonspiculated masses in terms of the density agrees with radiologists' general perception; namely, the benign masses in the nonspiculated category tend to have low image density, whereas the malignant masses in the nonspiculated category tend to have high image density for all three density measures. The ability to separate low-density benign masses from high-density malignant masses only in the nonspiculated category stresses the importance of using the density measures to differentiate between benign and malignant masses only after having excluded the spiculated masses.

Classification of Masses

The ability of each individual computer-extracted feature to aid in the differentiation between benign and malignant mass images was evaluated for the entire database with ROC analysis. The calculated A_z values are listed in Table 2. The ROC analysis shows that the spiculation measure outperformed the other features in distinguishing



b.



c.

between benign and malignant masses; the A_z value was 0.88 for spiculation compared with 0.54–0.65 for the other four features. We have therefore found that margin spiculation is as important a feature for the computerized method as it is for radiologists.

After the rule based on the spiculation measure (FWHM of 160°) was applied, the ability of these features to further distinguish between benign and malignant mass images in the remaining database (nonspiculated) was also studied with ROC analysis. The calculated A_z values for these features are listed in Table 2. As can be seen in Table 2, the spiculation measure is no longer a dominant feature in discriminating between benign and malignant masses in the nonspiculated category. The other four features perform better, however, in differentiating malignant from benign masses in the nonspiculated category than in the complete database (ie, both spiculated and nonspiculated). This finding indicates the importance of using these features to differentiate between benign and malignant masses only after the spiculated masses have been excluded.

Table 2
Performances of the Five Computer-extracted Features in Distinguishing between Benign and Malignant Mass Images

Feature	A ₂ for All 95 Mass Images	A ₂ for 36 Mass Images in the Nonspiculated Category
Margin		
Spiculation (FWHM)*	0.88	0.53
Sharpness*	0.56	0.68
Density		
Average gray level*	0.65	0.66
Contrast	0.59	0.70
Texture measure*	0.54	0.71

*These features were used as inputs in the ANN and the combined rule-based ANN classifiers.

Three automated classifiers were investigated for the task of merging the computer-extracted features into an estimate of the likelihood of malignancy: a rule-based method, an ANN, and a hybrid system. In determining the likelihood of malignancy for the cases that had both the mediolateral oblique and the craniocaudal views, the measurements obtained from both views were considered, and the view that the computer estimated had a higher likelihood of malignancy was used in the evaluation. For example, a mass would be classified as malignant if either one of the two views showed suspect signs (ie, either one of the FWHM measures from its two views satisfied the cutoff on the FWHM measure).

Rule-based method.—A rule-based method adapts knowledge from experts into a set of simple rules. Certain criteria for differentiating between benign and malignant masses have been established by expert mammographers (4,6,32). The rules used in our approach for measures of spiculation, margin sharpness, and density were based on these criteria.

A two-step rule-based method was studied for this database. Because of its clinical diagnostic importance, the spiculation measure was applied first in our rule-based method. After the spiculation measure (FWHM) was applied to identify spiculated masses (including some irregular masses) and categorize them as malignant first, a second feature was applied to characterize further the masses in the nonspiculated category as discussed in the previous section. To investigate the potential discriminant ability of the spiculation measure along with all the possible secondary features, we applied separately each of the remaining four features—the margin-sharpness mea-

sure and the three density measures—after the spiculation measure. The threshold of the spiculation measure (FWHM = 160°) was determined based on the entire database. The thresholds of the other four features were determined based on the remaining database only.

ANN.—The ANN approach is very different from the rule-based method. Instead of using predetermined empirical algorithms based on prior knowledge, ANNs are able to learn from examples and therefore can acquire their own knowledge through learning. Also, neural networks are capable of processing large amounts of information simultaneously. Neural networks do not, however, provide the user with explanations for their decisions and may not be able to bring preexisting knowledge into the network.

Here we used a conventional three-layer, feed-forward neural network with a back-propagation algorithm, which has been used in medical imaging and medical decision making (33,34). The structure of the neural network included four input units (each of which corresponded to a computer-extracted feature), two hidden units, and one output unit. The four features used as inputs to the ANN were the FWHM measure, the margin-sharpness measure, and two density measures (indicated by asterisks in Table 2). Similar performances were obtained when all three density measures were used. Because limiting the number of input features is critical in reducing the number of training samples needed, we kept the number of inputs to the ANN to a minimum; thus, only two density measures were used.

To determine the ability of our neural network to generalize from the training cases and make diagnoses for cases that had not been included in the database, we used a round-robin method, also known as the leave-one-out method. In this method, all but one of the cases were used to train the neural network. The single case that was left out was used to test the neural network. For the cases that had both mediolateral oblique and craniocaudal views, both images were left out in the round-robin training. The higher value of the two from the round-robin test was reported as the estimated likelihood of malignancy. This procedure was repeated for all the cases.

Hybrid system.—Each classifier has its advantages and limitations. With rule-based methods, one could adopt preexisting knowledge as rules. There are limitations, however, in the availability of knowledge and knowledge translation. Even the experts find it difficult to articulate particular types of “intuitive” knowledge, and the process of translating particular knowledge into rules is limited

by this expressive power. ANNs are capable of learning from examples and therefore can acquire their own knowledge. It may be most advantageous to use ANNs when intuitive knowledge cannot be explicitly expressed or is difficult to translate. The ANN needs a sufficiently large database, however, to learn effectively. Also, with an ANN there may be uncertainty as to whether the final learning goal is achieved in some situations.

To take advantage of both rule-based systems and ANNs in the task of classifying masses, we integrated a rule-based method and an ANN into a hybrid system. In the hybrid system, we initially applied a rule on the spiculation measure because both spiculated and irregular masses are highly suspect for malignancy. We then applied an ANN to the remaining masses. Basically, this method frees the ANN from having to "learn" the importance of spiculation to the detriment of learning the importance of the other features.

The threshold of the spiculation measure for the hybrid system was the same as the one used in the rule-based method. The ANN applied in the hybrid system was a three-layer, feed-forward neural network with a back-propagation algorithm that had a structure of three input units (corresponding to the three remaining features used in the ANN method), two hidden units, and one output unit. The same round-robin method was applied to test the generalization ability of this neural network to differentiate between benign and malignant masses in the nonspiculated category.

Observer Study

One experienced radiologist who specializes in mammography (D.E.W.) and five other radiologists with some experience in mammography participated in the observer study. The experienced radiologist characterized some features of the database after the observer study was completed. Three of the five other radiologists were general radiologists from Europe participating in visiting fellowships. At the time of the observer study, they had a total of 6 months to 2 years of experience in mammography. One of the remaining two was a fellow in mammography in his 3rd month of training. The fifth radiologist had 3 months of training in mammography (beyond the standard 2 months of training in residency) in a combination fellowship. In the study, each observer was asked to estimate the probability of malignancy for each of the 65 cases by using a 100-point scale based on the mammograms available. The performance of each observer in distinguishing between benign and malignant masses was

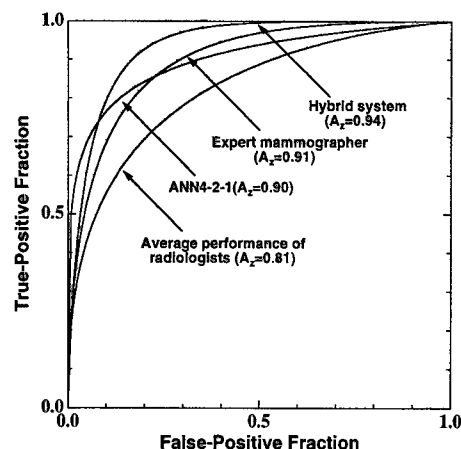


Figure 8. ROC curves for the performance of an experienced mammographer, five radiologists, the computerized scheme with ANN alone, and the computerized scheme with the hybrid system. ANN4-2-1 = ANN with four input units, two hidden units, and one output unit.

evaluated by using ROC analysis. An ROC curve was generated for the five less experienced radiologists as a group by averaging the two binormal parameters of their individual ROC curves (27,28).

RESULTS

Because the computer outputs from each individual classifier were monotonically correlated with the estimated probabilities of malignancy, we were able to evaluate the ability of each classifier to merge computer-extracted features into a correct estimated probability of malignancy based on the computer output with ROC analysis. The ROC curves of the ANN and hybrid system are shown in Figure 8. The A_z and the partial area index ${}_{0.90}A'_z$ values of the three classifiers are listed in Table 3. Among the three classifiers, the hybrid system yielded the highest A_z and ${}_{0.90}A'_z$ values. The specificities and positive predictive values of the three classifiers at 100% sensitivity were calculated. As shown in Table 3, the hybrid system yielded the highest specificity (69.2%), the two-step rule-based method the second highest (42.3%, 34.6%, 30.8%, 30.8%), and the ANN the third highest (19.2%).

The performance of the hybrid system was compared with that of the other two types of classifiers. No statistically significant difference ($P > .05$) was found for the A_z values based on the evaluation from the CLABROC program (35,36). Statistically significant differences for the

Table 3
Performances of the Three Classifiers in Distinguishing between the 26 Benign and the 39 Malignant Masses

Classifier	Specificity*	Positive Predictive Value*	Full Curve A_z	Partial Area Index	
				$_{0.90}A'_z$	P^\dagger
Two-step rule-based system (1st rule on FWHM)					
Margin sharpness	34.6%	69.6%	0.92	0.59	0.014
Average gray level	30.8%	68.4%	0.90	0.45	0.001
Contrast	30.8%	68.4%	0.92	0.58	0.021
Texture measure	42.3%	72.2%	0.92	0.63	0.015
ANN (4-2-1)	19.2%	65.0%	0.90	0.40	0.008
Hybrid system (rule-based and ANN 3-2-1)	69.2%	83.0%	0.94	0.73	...

Note.—ANN 4-2-1 = ANN with four input units, two hidden units, and one output unit; ANN 3-2-1 = ANN with three input units, two hidden units, and one output unit.

*Sensitivity was 100%.

† The P values were calculated for the difference in the $_{0.90}A'_z$ between the hybrid system and the other two classifiers.

Table 4
Performances of the Human Observers in Distinguishing between the 26 Benign and the 39 Malignant Masses

Observer	Specificity*	Positive Predictive Value*	Full Curve A_z	Partial Area Index	
				$_{0.90}A'_z$	
A	3.8%	60.9%	0.85	0.29	
B	11.5%	62.9%	0.86	0.37	
C	11.5%	62.9%	0.85	0.40	
D	0%	60.0%	0.70	0.07	
E	3.8%	60.9%	0.80	0.27	
Average performance of A-E	6.1%	61.5%	0.81	0.28	
Experienced mammographer	38.5%	70.9%	0.91	0.58	

*Sensitivity was 100%.

$_{0.90}A'_z$ values were found, however, at the levels of the two-tailed P values as listed in Table 3. Differences in positive predictive value and specificity at 100% sensitivity between the hybrid system and the two-step rule-based method on average were 13% and 34%, respectively. Differences in positive predictive value and specificity at 100% sensitivity between the hybrid system and the ANN were 18% and 50%, respectively.

The ability of each radiologist to distinguish between benign and malignant masses was determined based on the radiologist's subjective ratings of the probability of malignancy for the 65 cases. The ROC curves of the experienced mammographer and of the average performance of the five radiologists are shown in Figure 8. Table 4 lists their individual performances in terms of A_z , $_{0.90}A'_z$, positive predictive value, and specificity at 100% sensitivity. The average performance for the five radiologists was calculated (Table 4). The experienced mam-

mographer had an A_z of 0.91, whereas the average of the five radiologists yielded an A_z of 0.81. The partial area index $_{0.90}A'_z$ for the experienced mammographer was 0.58, whereas the partial area index $_{0.90}A'_z$ for the five radiologists was 0.28. Student t test for paired data was employed to evaluate the statistical significance of these differences (16). Results showed the differences in A_z and $_{0.90}A'_z$ to be statistically significant (two-tailed P values of .032 and .006).

The ability of the observers to distinguish malignant from benign masses was compared with that of the computerized method using the hybrid system. The differences in A_z and $_{0.90}A'_z$ between the experienced mammographer and the computerized method were found to be not statistically significant (two-tailed P values of 0.38 and 0.30) based on the evaluation from the CLABROC program (35,36) and the modified version of the CLABROC program (30). Results of the Student t test for paired data

showed that the differences in A_z and $_{0.90}A'_z$ between the average performance of the five radiologists and the computerized method were both statistically significant (two-tailed P values of .0131 and .0015). Furthermore, statistically significant differences were found between the two in terms of the positive predictive value and the specificity at the 100% sensitivity level (two-tailed P values < .0001).

The differences in positive predictive value and specificity at 100% sensitivity between the average performance of the five radiologists and the performance of the experienced mammographer were 9% and 32%, respectively; these differences were also found to be statistically significant. The differences in positive predictive value and specificity at 100% sensitivity between the average performance of the five radiologists and that of the computerized scheme were even larger, 21% ($P < .0001$) and 63% ($P = .0001$), respectively. In other words, with the database we used, at a 100% sensitivity level (ie, no loss of malignant cases), the average radiologists misclassified or essentially overcalled 24 of the 26 benign cases, whereas the computer scheme misclassified only eight of the 26 benign cases.

DISCUSSION

We have developed a computer scheme that automatically extracts features of masses that are similar to those perceived by radiologists. Feature analysis has indicated that our computer-extracted features correlate well with the major features perceived by radiologists, as shown in Figures 4, 5, and 7. We have shown that spiculation (FWHM measure) is a dominant feature for analysis by both radiologists and computerized methods.

The shape of a mass can be described as regular or irregular, lobulated or not lobulated, circular or ovoid. Generally, shape is not as important as margin characteristics in the determination of the benign versus malignant status of a mass. An irregular shape can, however, be a useful sign of malignancy. We did not use a single measure to directly characterize the shape of a mass in our scheme. However, one can correctly identify irregular masses as suspicious for malignancy based on the spiculation measure, because the direction of the maximum gradient along the margin of an irregularly shaped mass can vary as greatly as that of a spiculated mass. A lobulated mass also has a higher spiculation value than a smooth circular or ovoid mass because the direction of the maximum gradient relative to the radial direction

along the margin of a lobulated mass varies more than that along the margin of a smooth mass. Thus, a smooth lobulated mass will be ranked as more suspect for malignancy than a smooth circular or ovoid mass, similar to the rank ordering radiologists would give. Some lobulated masses might be classified into the spiculated category if they were very highly lobulated.

We have studied three types of classifiers with which to merge the computer-extracted features. The three classifiers mimic three possible ways that radiologists might merge the information that they perceive in the task of classification of masses. The combination of the rule-based method by using the spiculation measure with the ANN is probably the one that serves this task best for several reasons. First, introduction of the well-known importance of spiculation, which was also shown here, into our system with a one-step rule-based method allows the ANN to "concentrate" on acquiring its own knowledge for the more difficult features for which considerable overlap in the appearance of benign and malignant masses occurs. Second, the good correlation between the computer spiculation measure and an expert mammographer's spiculation ratings, as well as the similar performance of the two in distinguishing between benign and malignant masses, allows a reliable translation of the "intuitive" knowledge into a simple rule in the hybrid system. Third, in clinical practice, radiologists are more likely to process the information they perceive in the same way that is used in our hybrid system, namely, examining for spiculation, the only truly diagnostic feature for malignancy, first and then analyzing all the possible secondary features to determine the likelihood of malignancy.

We evaluated the classifiers by using self-consistency and round-robin methods. The consistency method yielded A_z values of 0.92, 0.93, and 0.98 for the two-step rule-based method, the four-input ANN, and the hybrid system, respectively. The round-robin evaluation was performed to test the generalization ability of the classifiers. The two-step rule-based method was investigated only to understand the features, and so we did not proceed with round-robin testing of this method. The round-robin evaluation of the four-input ANN yielded an A_z value of 0.90. The evaluation of the hybrid system with round-robin analysis on the three-input ANN yielded an A_z of 0.94. The rule was set on the spiculation measure in the hybrid system because spiculation is the major feature used intuitively by radiologists in predicting malignancy, and this rule did not undergo round-robin analysis. In ad-

dition, the aim of the spiculation measure was not to separate malignant masses completely from benign masses but to identify only those masses that were very likely to be malignant.

Generalization of a trained network is influenced by three factors: the size and efficiency of the training set, the architecture of the network, and the physical complexity of the problem. Round-robin method is one of the ways to validate a trained network on a data set different from the one used in the training. A valid generalization, however, can be guaranteed only when the training set size is sufficiently large relative to the architecture of the network (37). We are aware of the inadequacies of using a finite database, which is usually what is available in the medical field, and thus we provided details about the characteristics of the clinical database (Fig 1) used in the study.

Of the three types of classifiers, the hybrid system performed the best in differentiating malignant from benign masses. One could expect that the performance of the ANN would be similar to that of the hybrid system because they both use the same four features as the inputs. Of the three classifiers, however, the ANN performed the worst in terms of A_z , $_{0.90}A_z'$, and the performance at 100% sensitivity. Although the difference in A_z between the hybrid system and the ANN was not statistically significant (two-tailed P value of .2), the difference in performance between the two classifiers at the high sensitivities ($_{0.90}A_z'$) was found to be statistically significant (two-tailed P value of .008). This difference resulted from the dominant nature of the spiculation measure, which kept the ANN-alone method from learning the importance of the other three features in differentiating subtle malignant masses from benign masses (38). It seems that only when the ANN was used after the spiculation criterion did it learn to effectively interpret the complicated interrelationship among the remaining features in determining the benign or malignant status of the subtle cases. With an unlimited database, the ANN-alone method might learn as well as the combined rule-based ANN method in distinguishing between benign and malignant masses (both spiculated and nonspiculated). Nevertheless, it was still more efficient to bring well-known knowledge directly into a classifier to avoid lengthy training times, the need for larger databases, and uncertainty in whether the final learning goal (well-known rules) would be achieved.

The performances of the expert mammographer and our computerized classification scheme were significantly better than the average performance of radiologists with

less mammographic experience, and this difference was even greater at the high sensitivity levels (P values ranging from .013 to <.001). Variability in radiologists' interpretations of mammograms is due to the differences in their knowledge and experience and has been demonstrated in our observer study and in other's work (39). The superior performance of the computerized classification scheme in distinguishing malignant masses from benign masses, especially at high sensitivity levels, emulates the performance of an expert mammographer. This finding underscores the potential usefulness of a computer-aided diagnosis classification scheme as an aid to improving the performance of less experienced mammographers and thus reducing the variability among radiologists in their mammographic interpretation and reducing the number of biopsies performed for benign masses.

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